

Computationally Efficient Operation of Power Flow Controllers

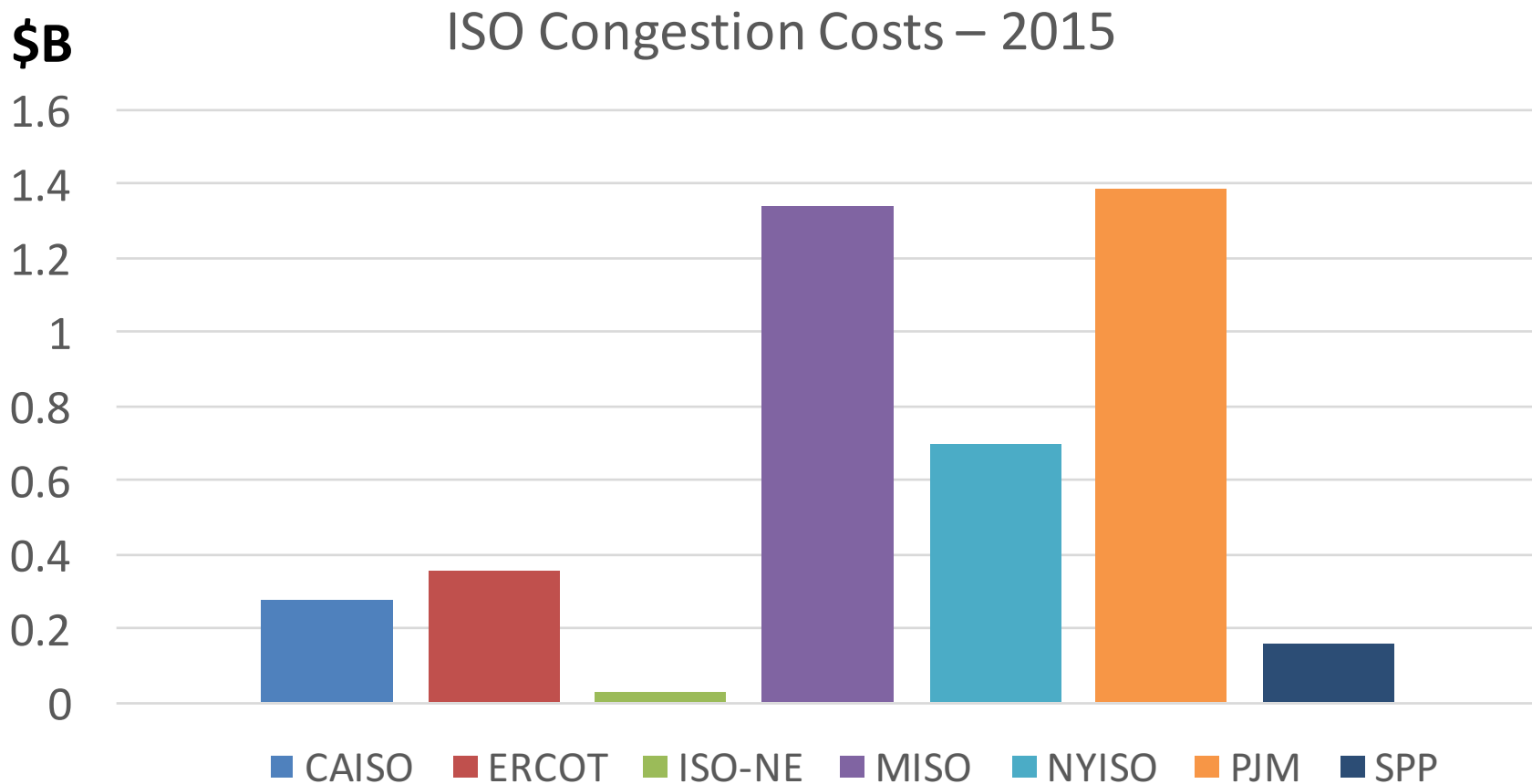
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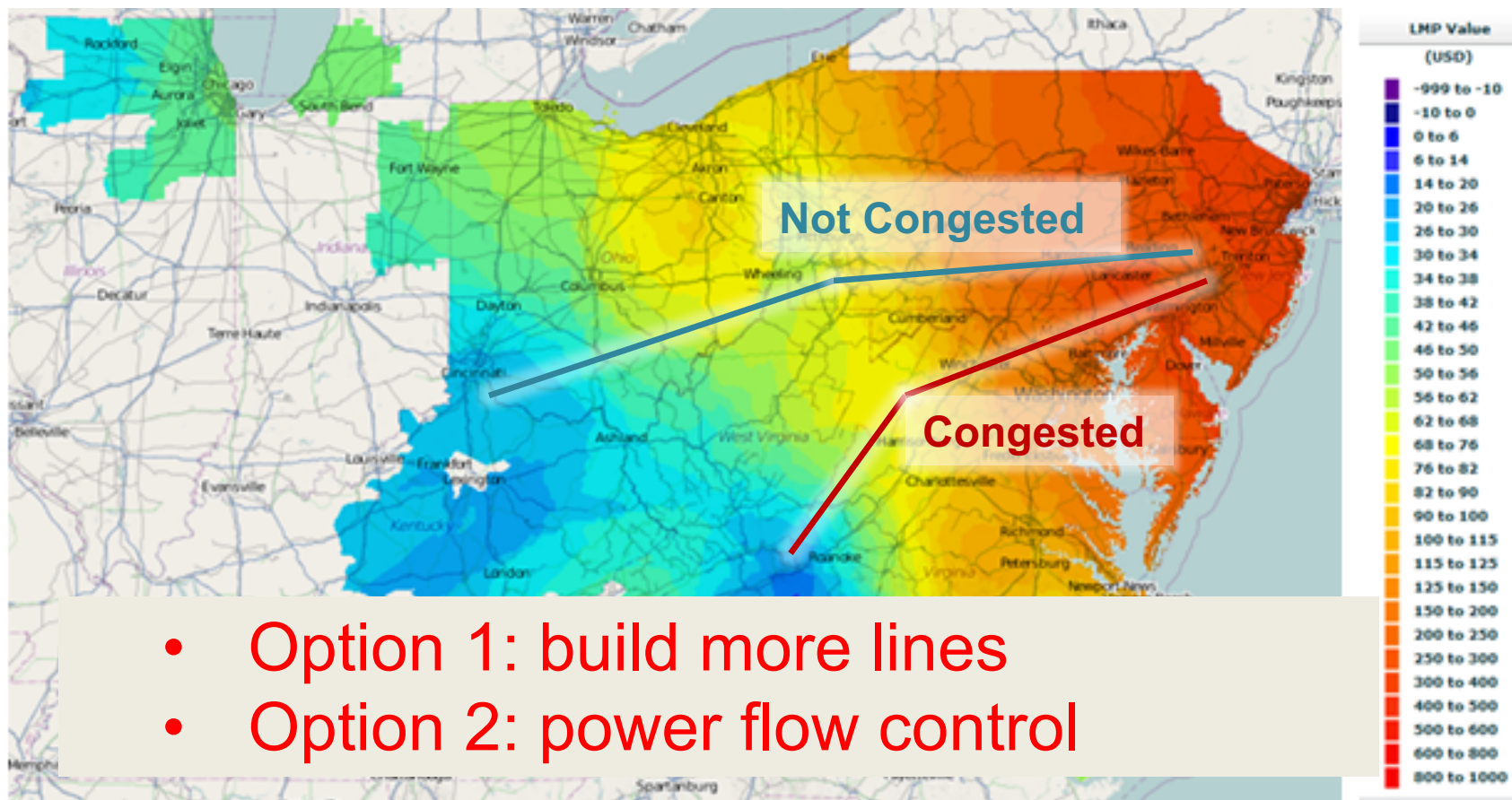
University of Utah



Congestion Cost in US ISO/RTOs

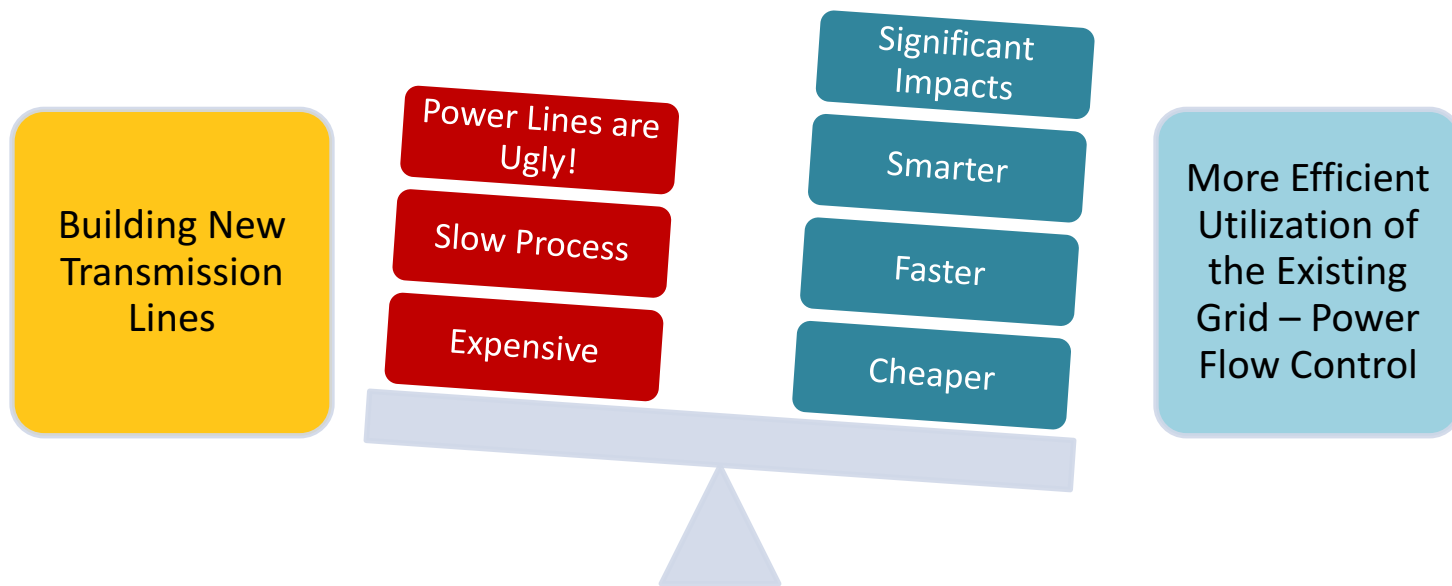


Transmission Bottlenecks



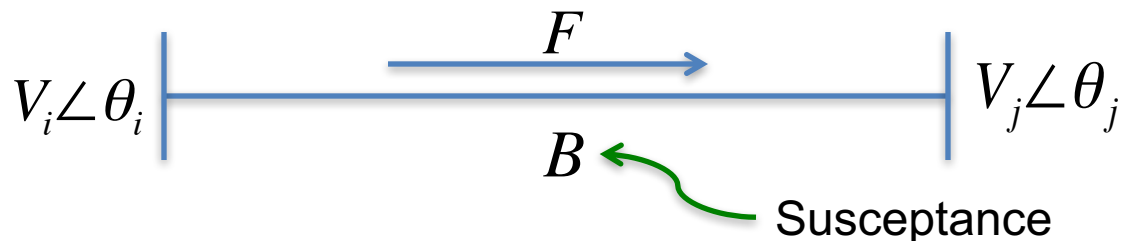
- Option 1: build more lines
- Option 2: power flow control

Choices



More efficient utilization of the existing network is cheaper and paramount!

Power Flow Physics



Electricity flows according to the laws of physics, not economics!

DC Power Flow Equation

$$F = B(\theta_j - \theta_i)$$

This is a linear approximation of AC power flow equation:

- Relatively accurate
- Facilitates efficient computation

$$F_k = B_k (\theta_j - \theta_i)$$

$$B^{\min} \leq B \leq B^{\max}$$

Variable Impedance FACTS

Nonlinear →

Computational Burden

Power Flow Physics

Computational Burden

Susceptance

Electricity flows according to the laws of physics, not economics!

**No FACTS set point adjustment
within EMS or MMS software**

- Facilitates efficient computation

$$F_k = B_k (\theta_j - \theta_i)$$

Variable Impedance FACTS

$$B^{\min} \leq B \leq B^{\max}$$

Nonlinear →

Infrequent ad hoc adjustments

Technology – TCSC

- Thyristor-Controlled Series Compensator

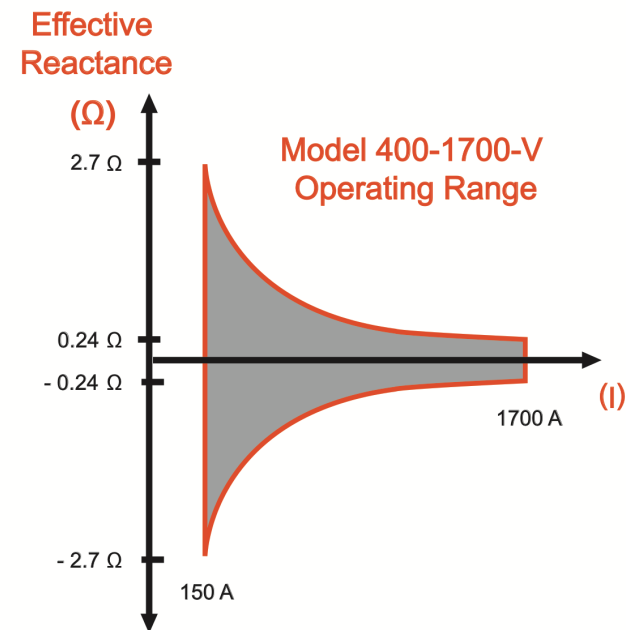


ABB – TCSC brochure

Technology – Smart Wires



Power Router brochure

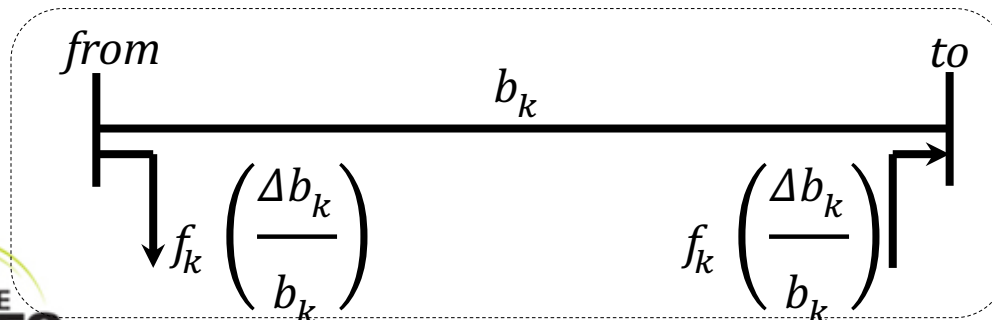
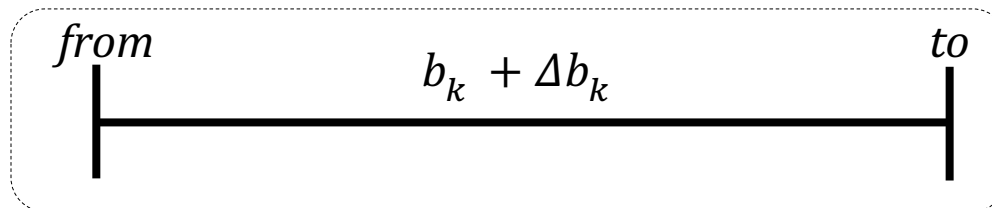


Objective:

**Design a Computationally-
efficient Algorithm to Control
the Power Flow Controller
Set Points**

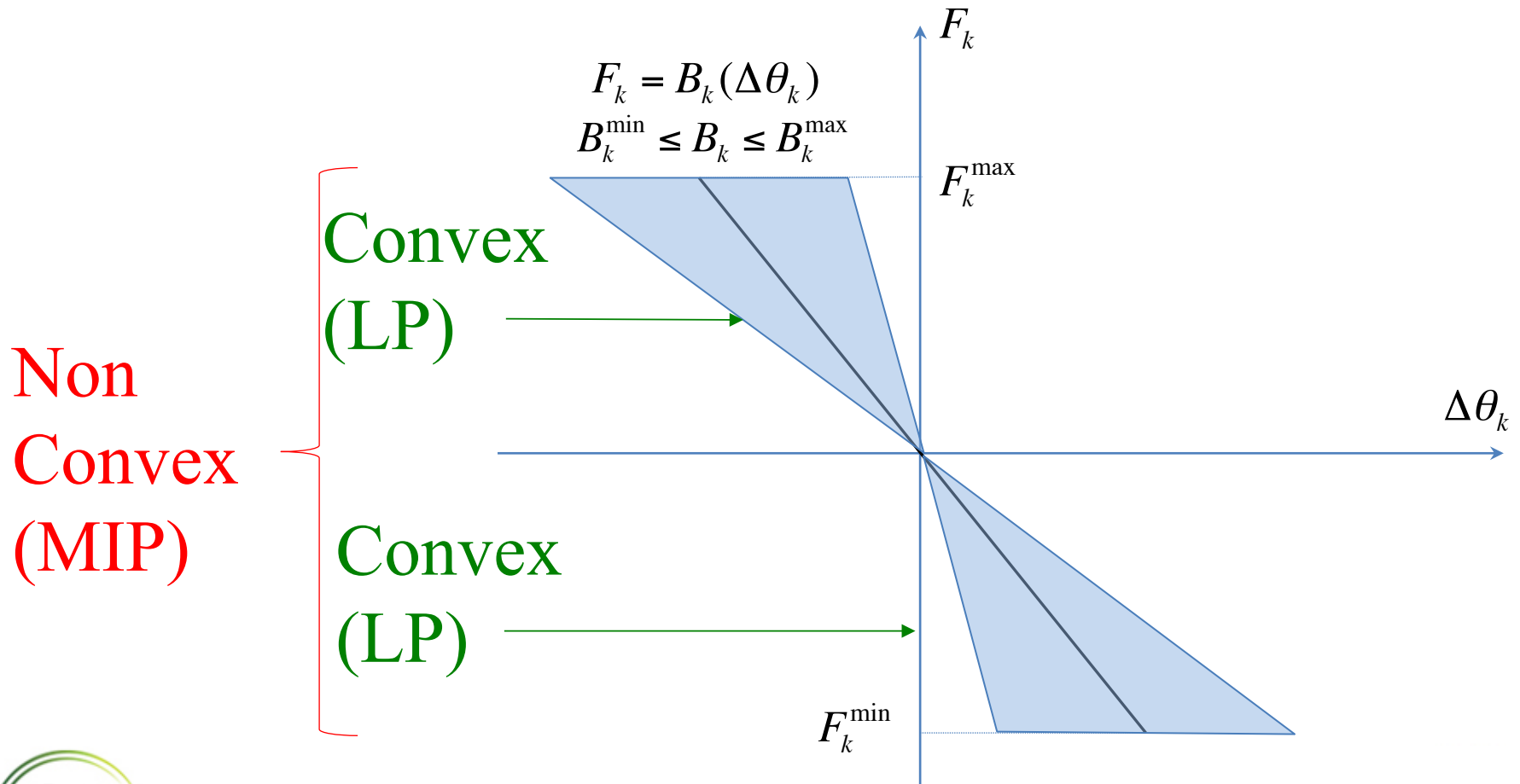
Shift Factor Structure

- Industry implementations of SCUC and SCED do not use $B - \theta$ structure; they use PTDFs.
 - No need to model all the voltage angles
 - No need to calculate all the flows
 - Significantly faster compared to $B\theta$



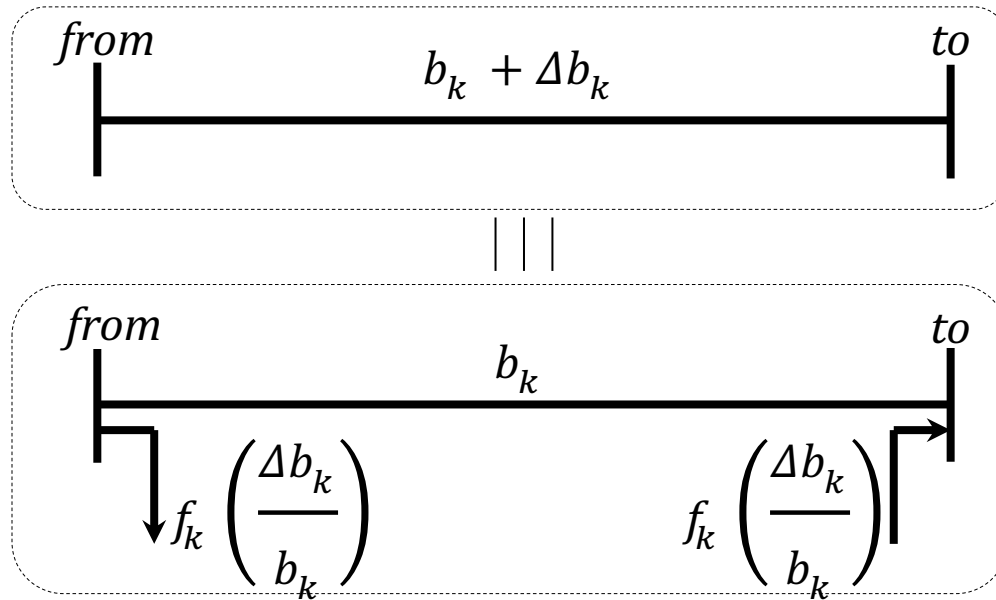
The injection pair involves NONLINEAR terms.

Computational Complexity – NLP/MILP



What if we knew which B&B tree node is the optimal node?

Reformulation to an MILP



$$\psi_k = \frac{f_k \Delta b_k}{b_k}$$

$$f_k \geq 0: \quad \frac{f_k \Delta b_k^{\max}}{b_k} \leq \psi_k \leq \frac{f_k \Delta b_k^{\min}}{b_k}$$

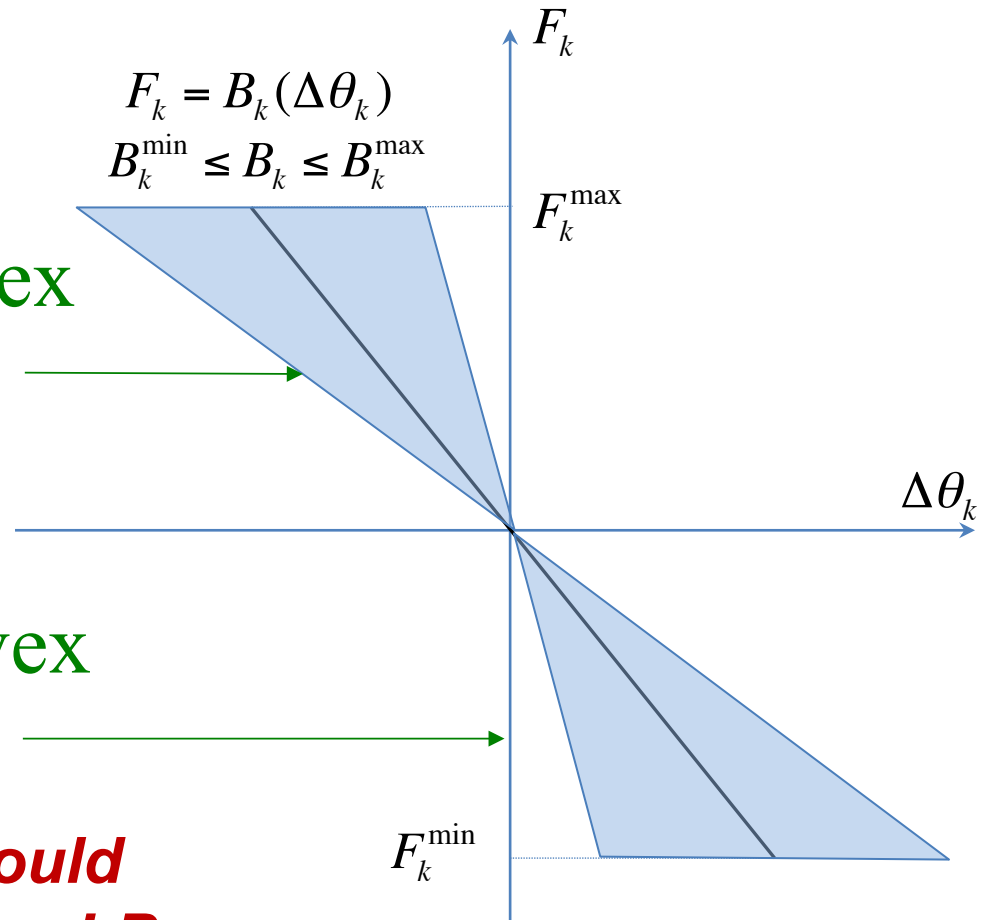
$$f_k \leq 0: \quad \frac{f_k \Delta b_k^{\max}}{b_k} \leq \psi_k \leq \frac{f_k \Delta b_k^{\min}}{b_k}$$

Engineering Insight

- We only need to know the direction of the power flow
- We know this direction for major lines (COI)
- *Even if we do not know the direction, we can run a two-stage DCOPF and identify it.*

Convex
(LP)

Convex
(LP)



Knowing the direction would reduce the complexity to a LP

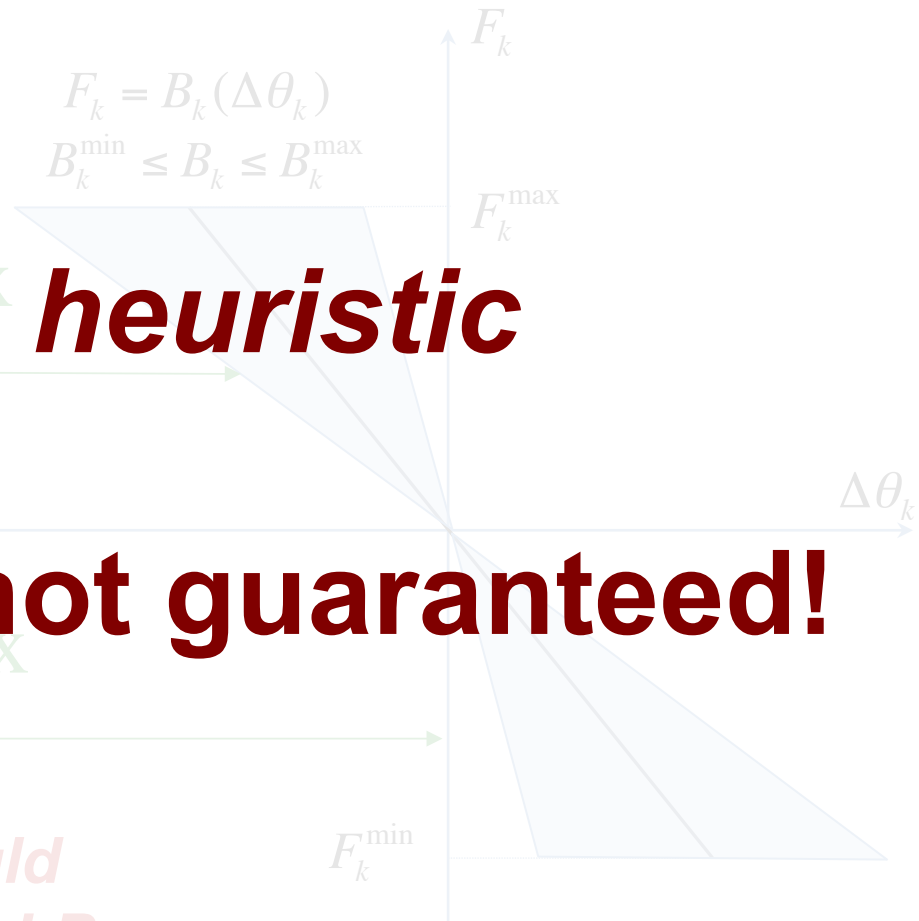
Engineering Insight

- We only need to know the direction of the power flow
- We know this direction for major lines (CO)
- *Even if we do not know the direction, we can run a two-stage DCOPE and still*

This is a heuristic

Optimality is not guaranteed!

Knowing the direction would reduce the complexity to a LP

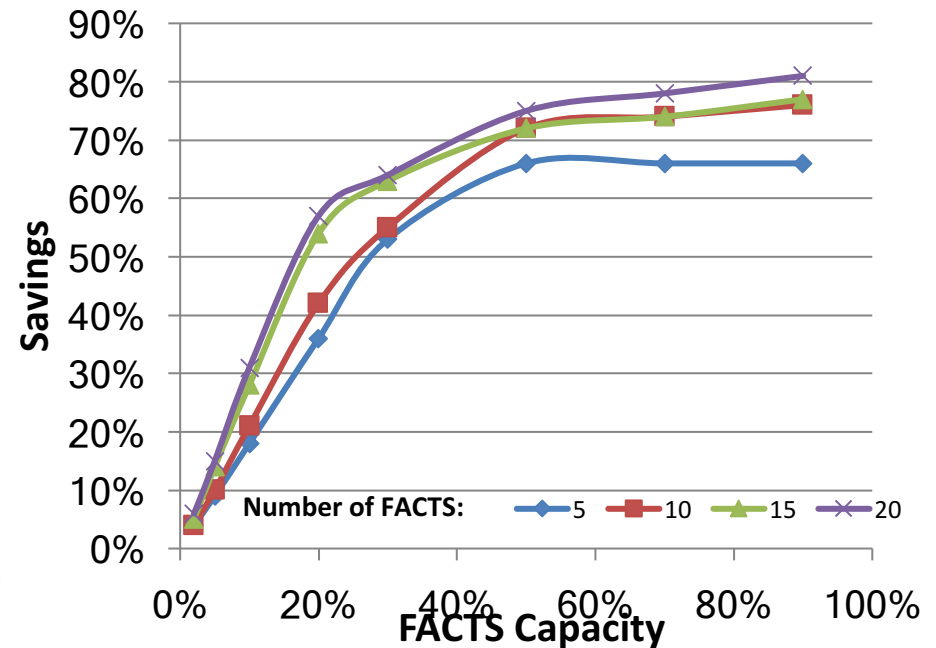
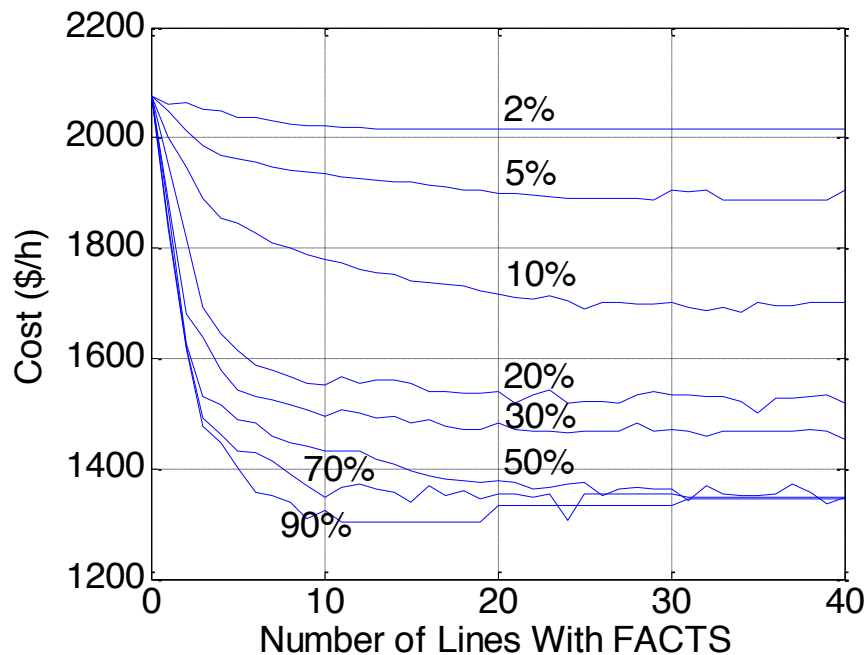


SCED Cost Savings—IEEE 118-Bus System

Savings are calculated compared to a transportation model

Optimal FACTS Placement:
>98% Optimal

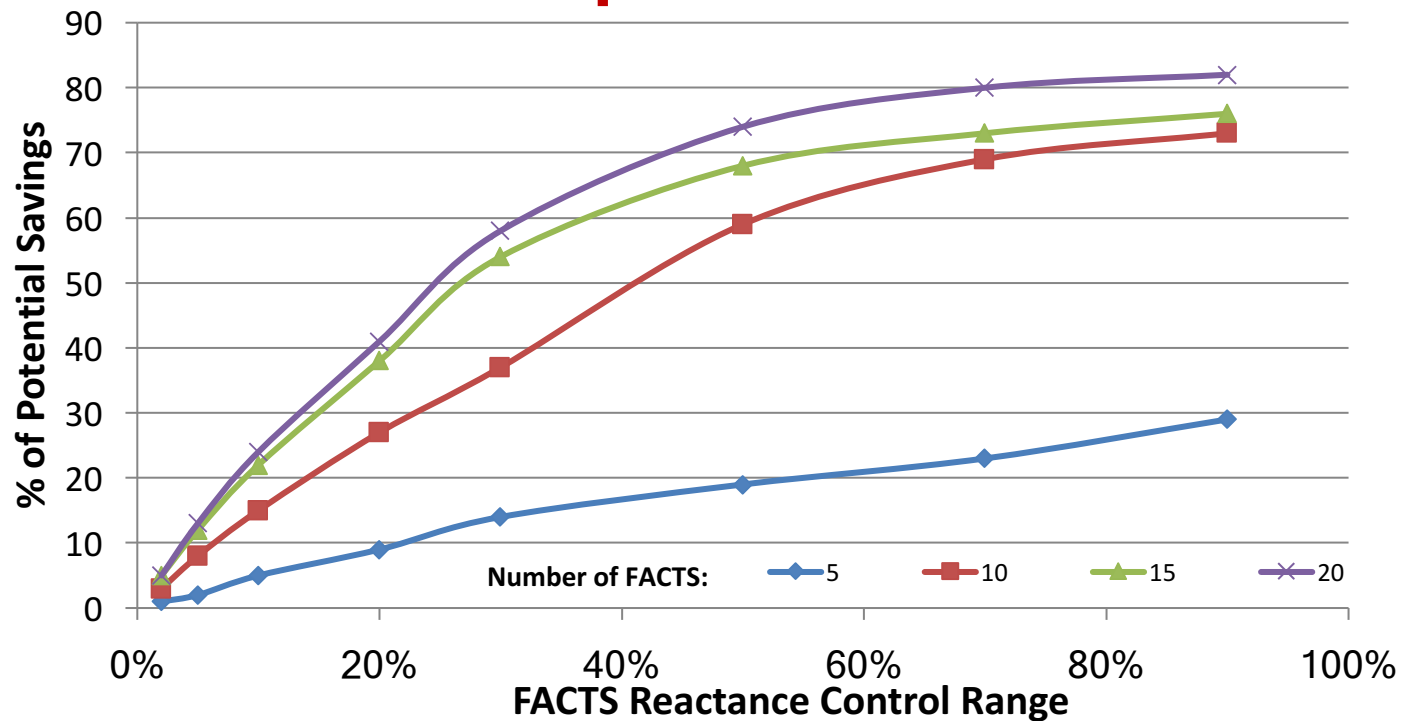
Located on More Heavily
 Utilized Lines: **100% Optimal**



SCED Cost Savings—Polish System

**Located on More Heavily Utilized Lines:
100% Optimal**

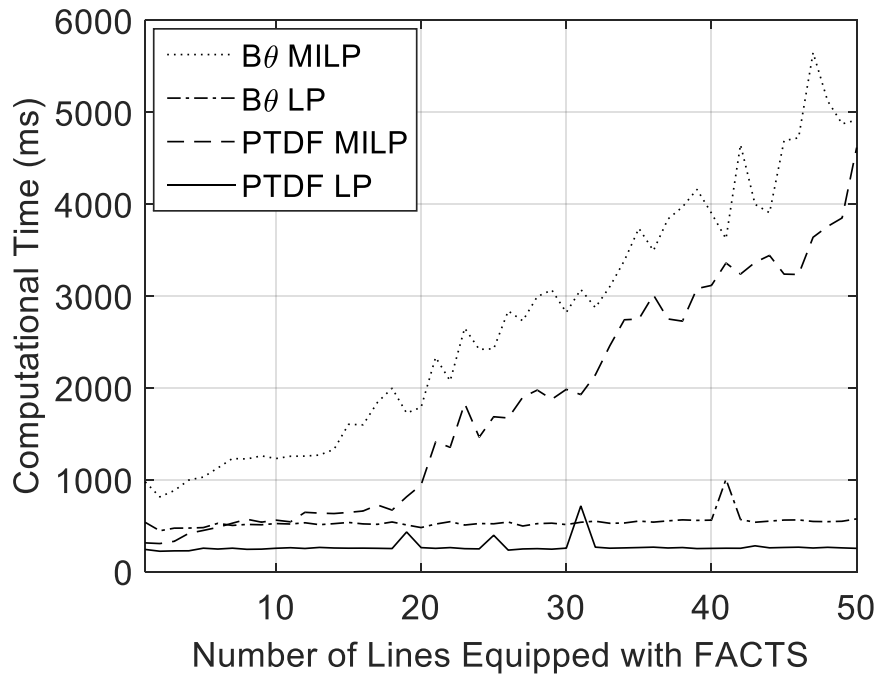
~2,400 buses
~2,900 branches



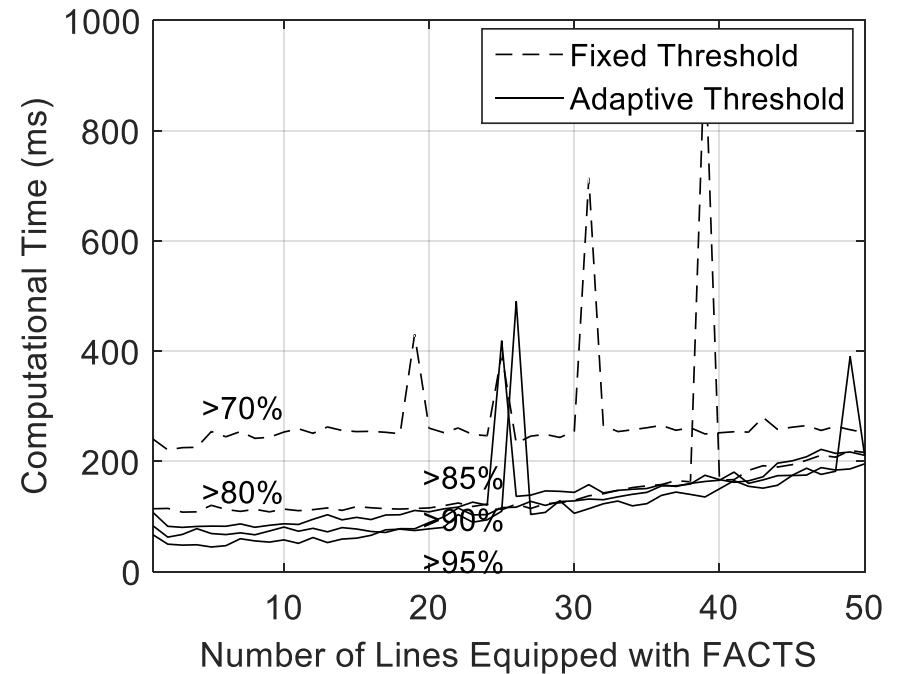
Savings are calculated compared to a transportation model

Results – Polish System

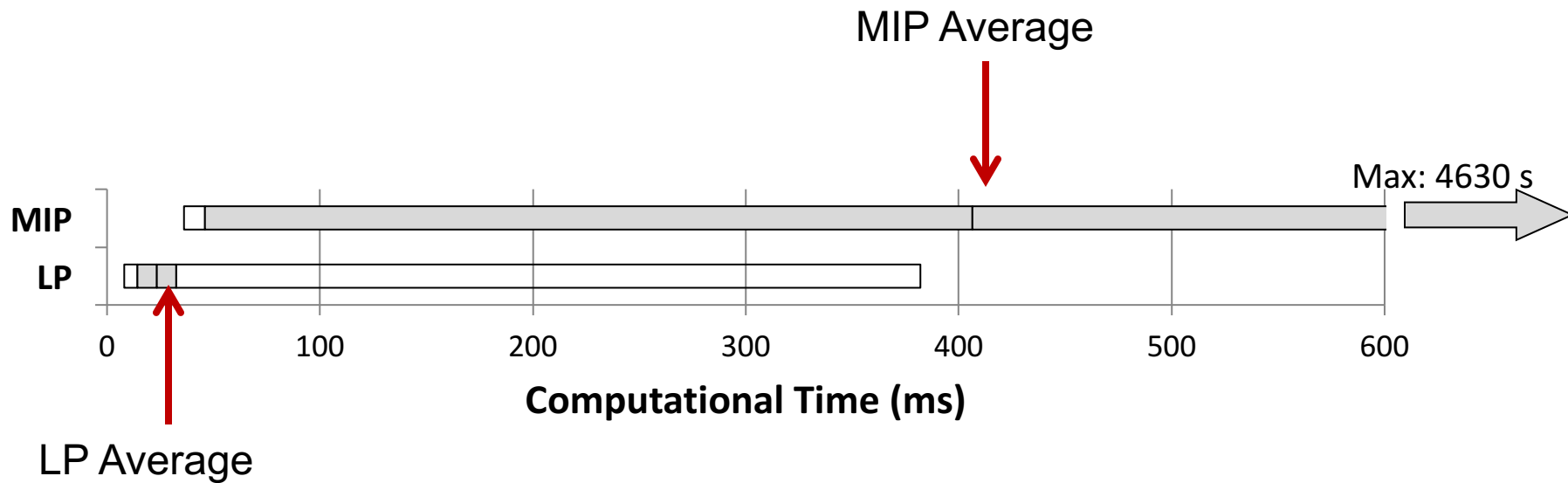
$B\theta$ versus PTDF



Fixed versus Adaptive Thresholds

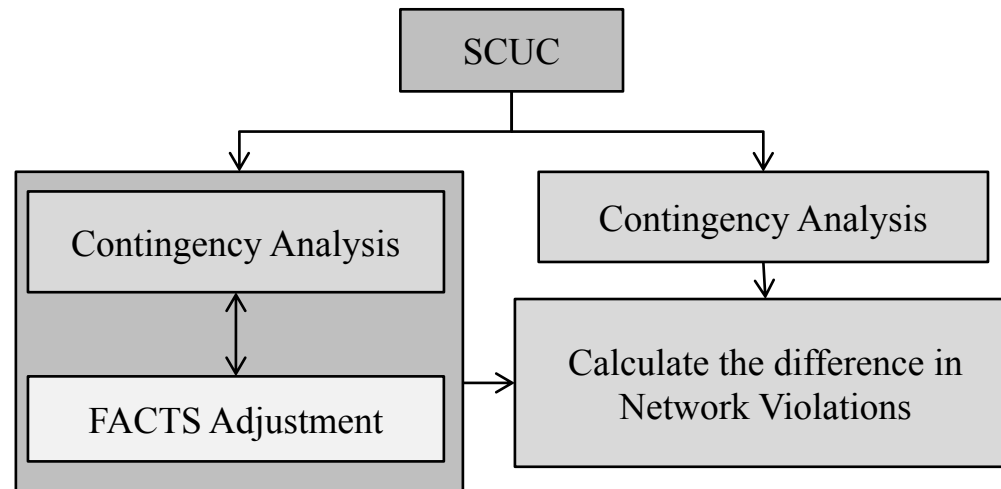


Computational Time

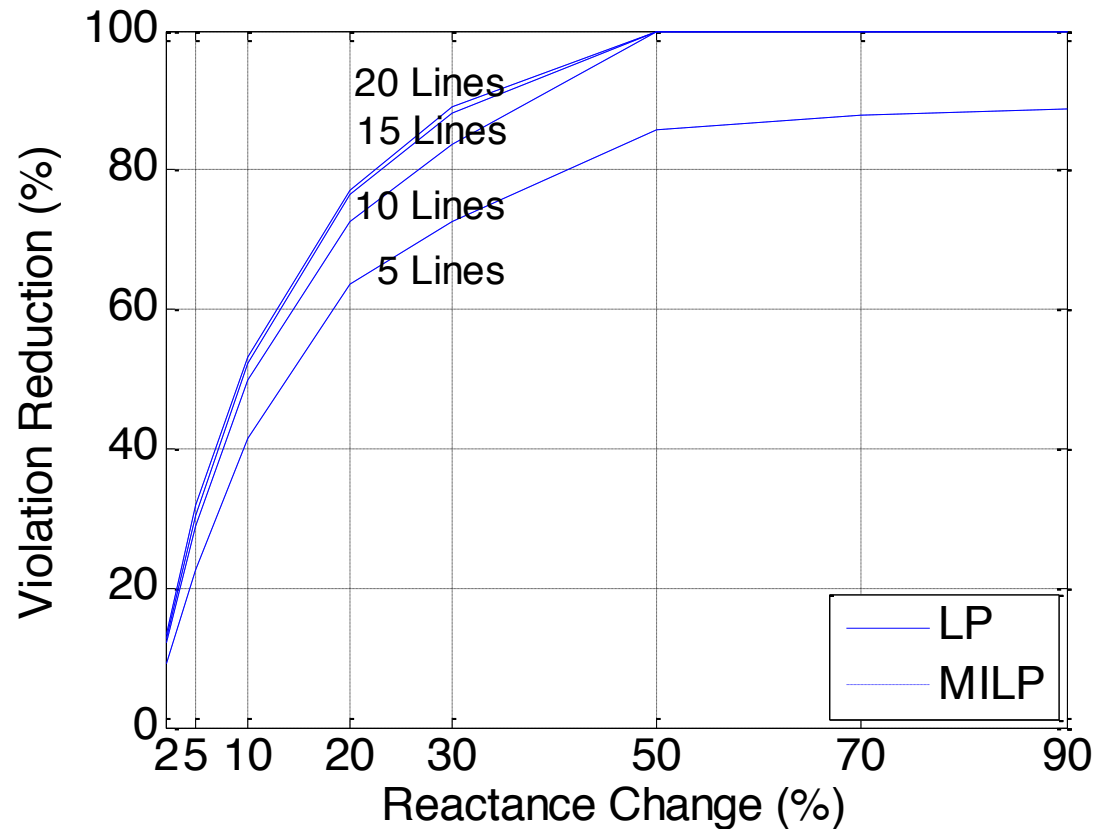


Corrective Adjustments

- In corrective adjustments we have even better insight about the direction of the power flow: pre- or post- contingency flows
- Goal: minimization of post-contingency network violations
- **Optimal utilization of FACTS in recourse state only**



Corrective Results—IEEE 118-Bus System



Located on More
Heavily Utilized
Lines:
100% Optimal

Conclusions

- Mathematical representation of OPF with FACTS: NLP
- We reformulated the NLP to a MILP; using our knowledge of electricity flow physics, we reformulate the problem to an LP
- The LP heuristic is extremely effective: it found the optimal solution more than 98% of the time.
- The heuristic is extremely fast (LP) and would not add to the complexity of the OPF problem

Questions?

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- M. Sahraei-Ardakani and K. Hedman, "A Fast LP Approach for Enhanced Utilization of Variable Impedance Based FACTS Devices," *IEEE Transactions on Power Systems*
- M. Sahraei-Ardakani and K. Hedman, "Day-Ahead Corrective Adjustment of FACTS Reactance: A Linear Programming Approach," *IEEE Transactions on Power Systems*
- M. Sahraei-Ardakani and S. Blumsack, "Transfer Capability Improvement through Market-Based Operation of Series FACTS Devices," *IEEE Transactions on Power System*
- M. Sahraei-Ardakani and K. Hedman, "Computationally Efficient Adjustment of FACTS Set Points in DC Optimal Power Flow with Shift Factor Structure," *IEEE Transactions on Power*