



Operation of Power Flow Controllers: Computational Efficiency and Market Participation

Mostafa Sahraei-Ardakani

mostafa.ardakani@utah.edu



Summary of Research Projects

- Power System Operation During Windstorms
 - Collaborative Research with Department of Civil Engineering
- Computationally-Efficient Algorithm Design for Operation of Power Flow Controllers
 - Transmission Switching (ARPA-E Project)
 - Controllable Reactance (TCSC, Smart Wire Grid)
- Market Design for Flexible Transmission



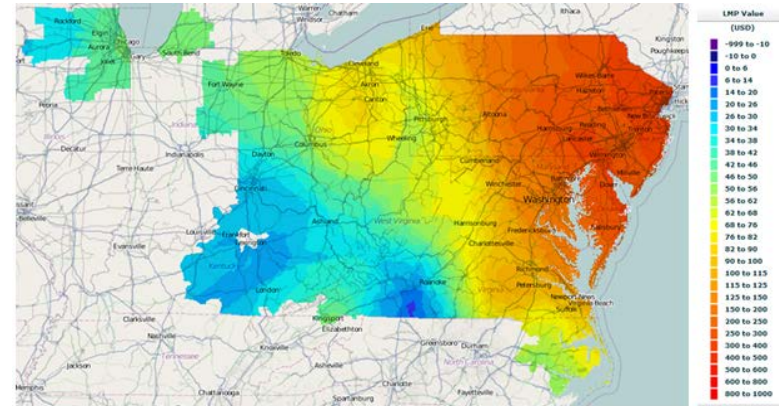
Motivation



Economic size of the industry: \$350 billion



Transmission system is under stress

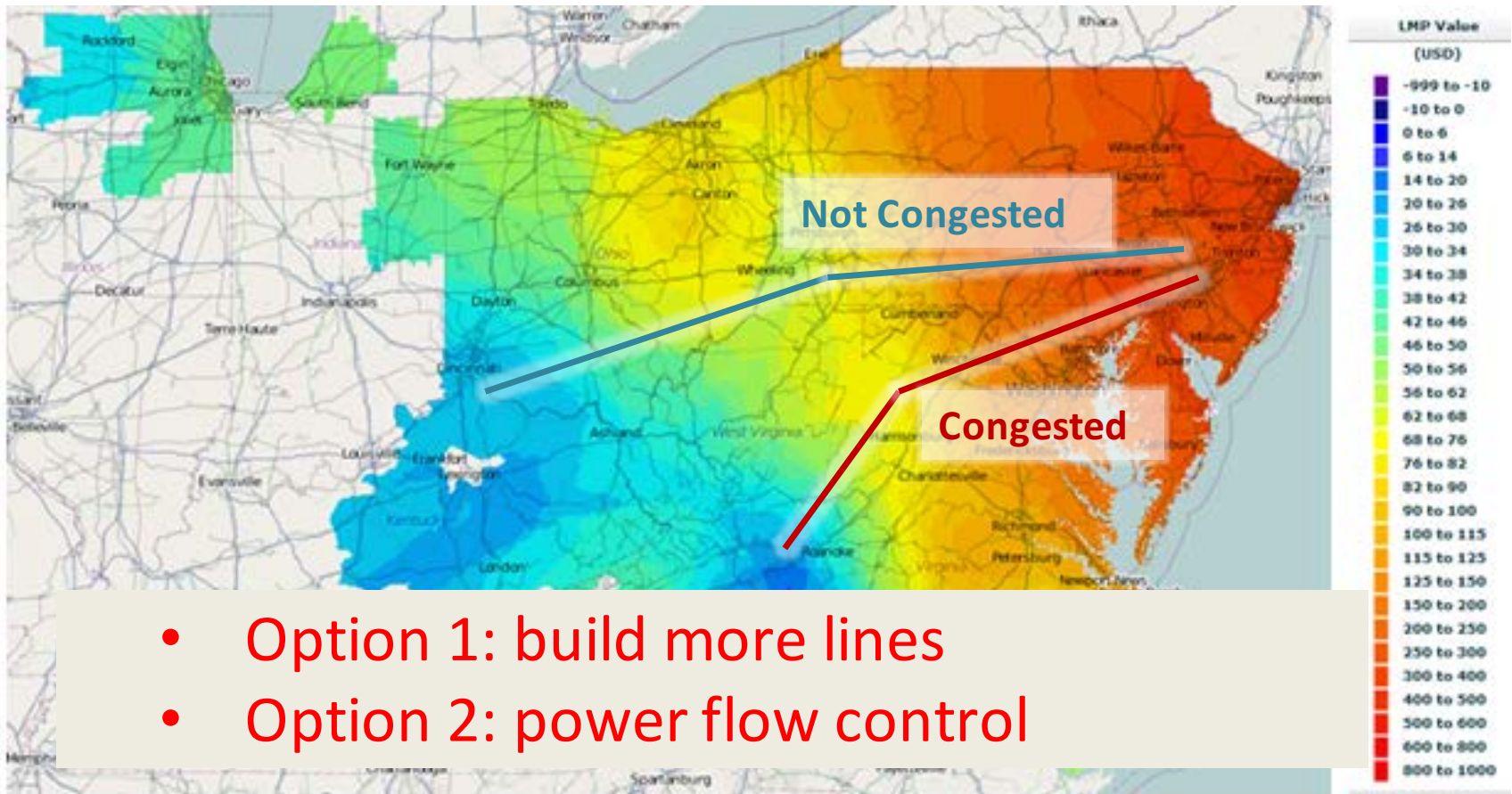


Transmission bottlenecks create economic inefficiency

Transmission system needs to be upgraded

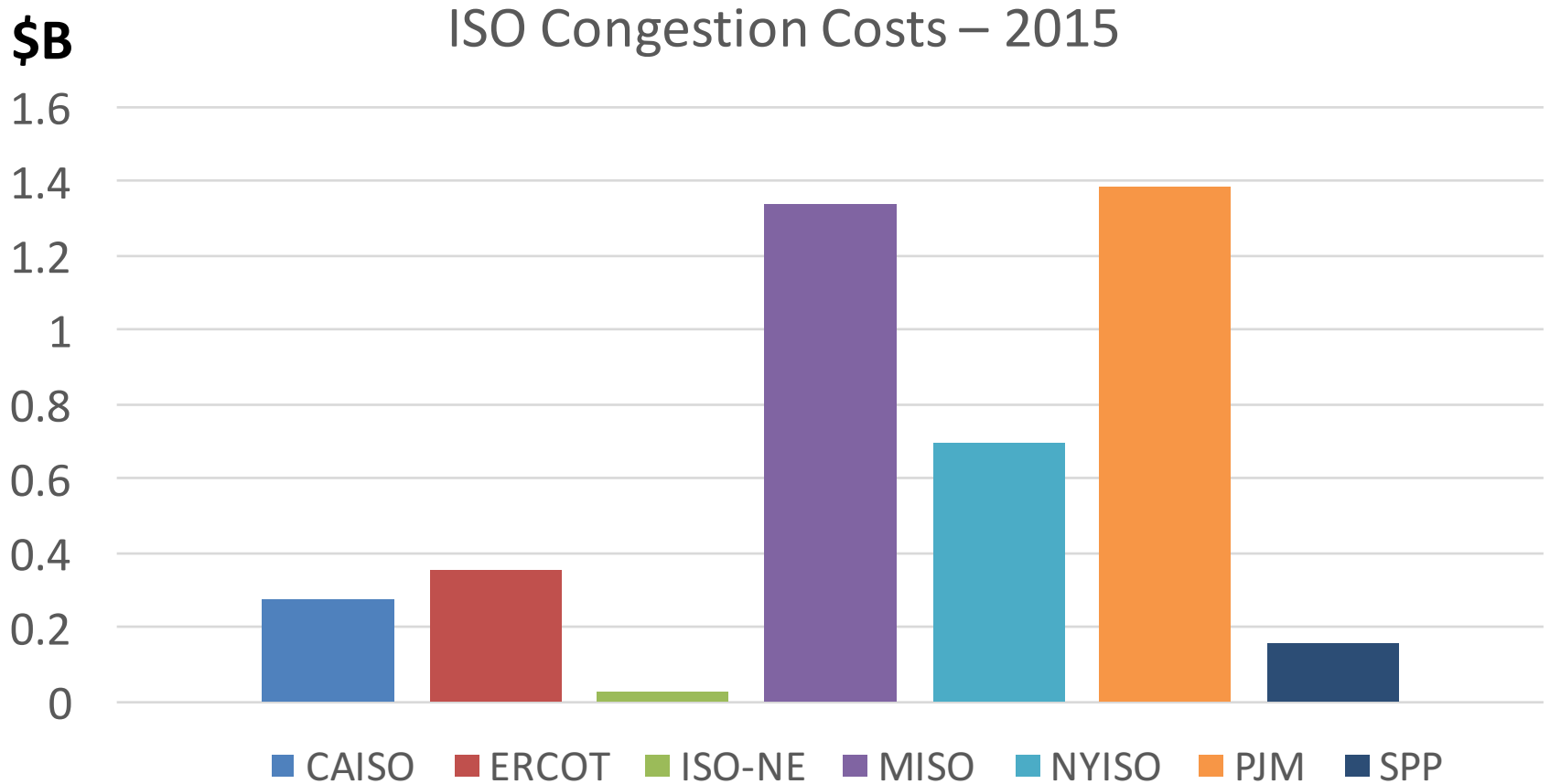
- Improved economic efficiency
- Reliability-motivated upgrades

Transmission Bottlenecks



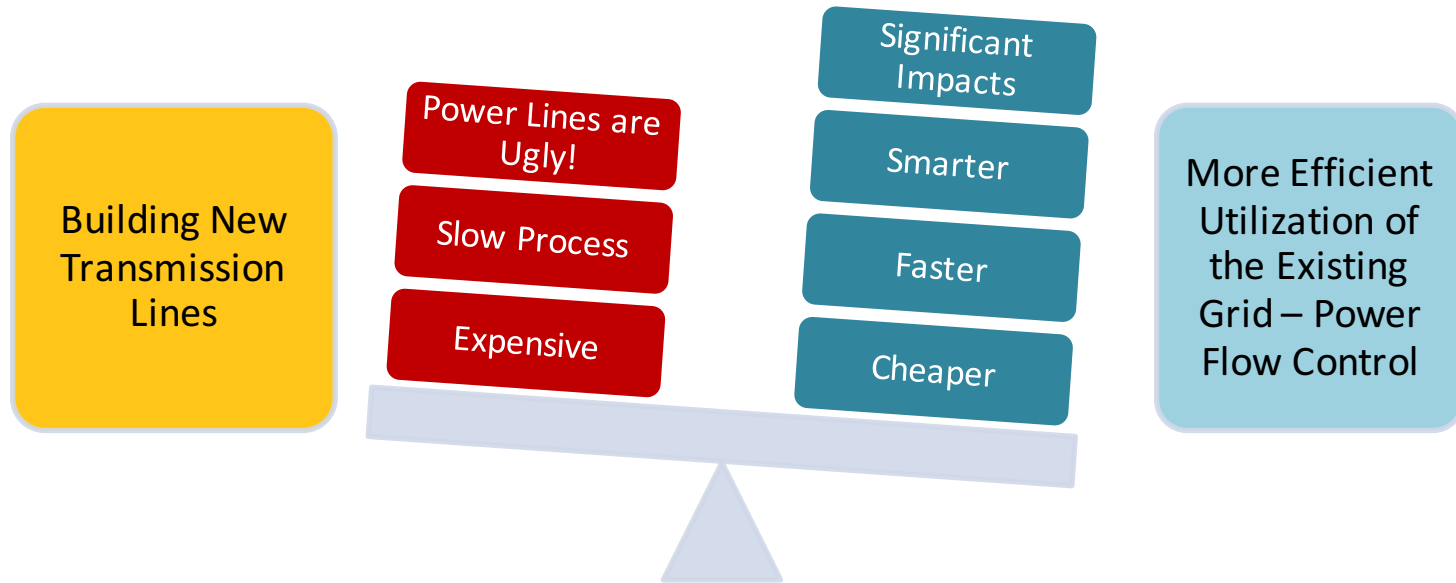


Congestion Cost in US ISO/RTOs





Choices



More efficient utilization of the existing network is cheaper and paramount!



Research and Development Efforts

- ARPA-E GENI initiative: Over 40 million dollars for power control hardware and software

Hardware:

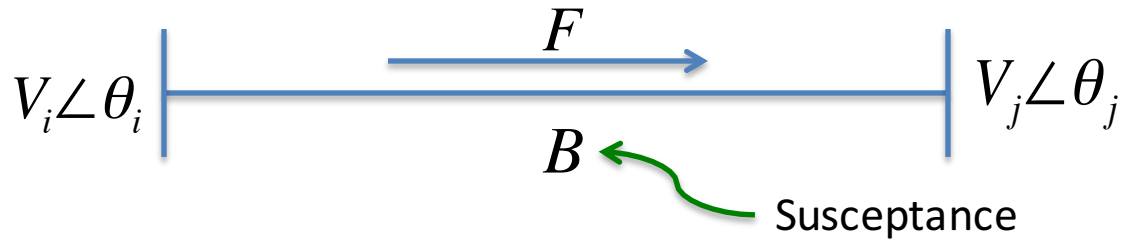
- Smart wire grid device
- Flexible AC Transmission System (FACTS)

Software:

- Transmission switching (TS)
 - Fast convergence
 - Quality AC solution
 - Dynamic stability analysis
- **Enhanced FACTS adjustment (not supported by ARPA-E)**
 - Same benefits
 - More or less the same concerns



Power Flow Physics



Electricity flows according to the laws of physics, not economics!

DC Power Flow Equation

$$F = B(\theta_j - \theta_i)$$

This is a linear approximation of AC power flow equation:

- Relatively accurate
- Facilitates efficient computation

$$\left\{ \begin{array}{l} F_k = B_k(\theta_j - \theta_i) \\ B^{\min} \leq B \leq B^{\max} \end{array} \right.$$

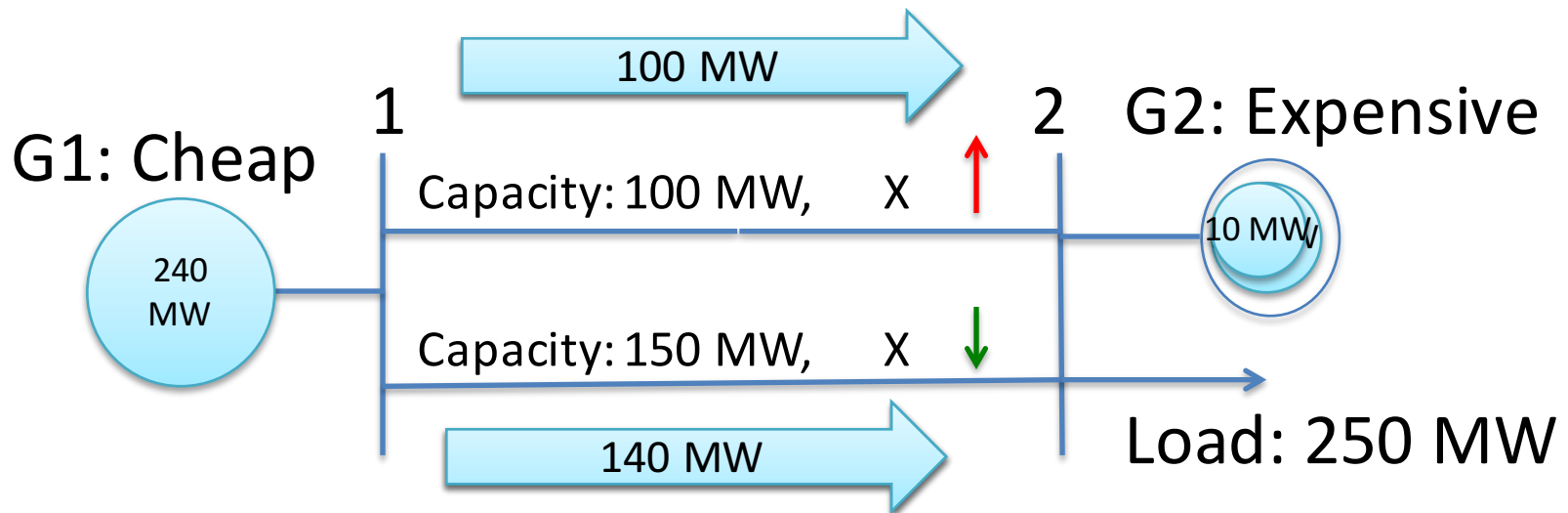
Variable Impedance FACTS

Power Electronics



Economic Example

Cost Reduction!



Technology – TCSC

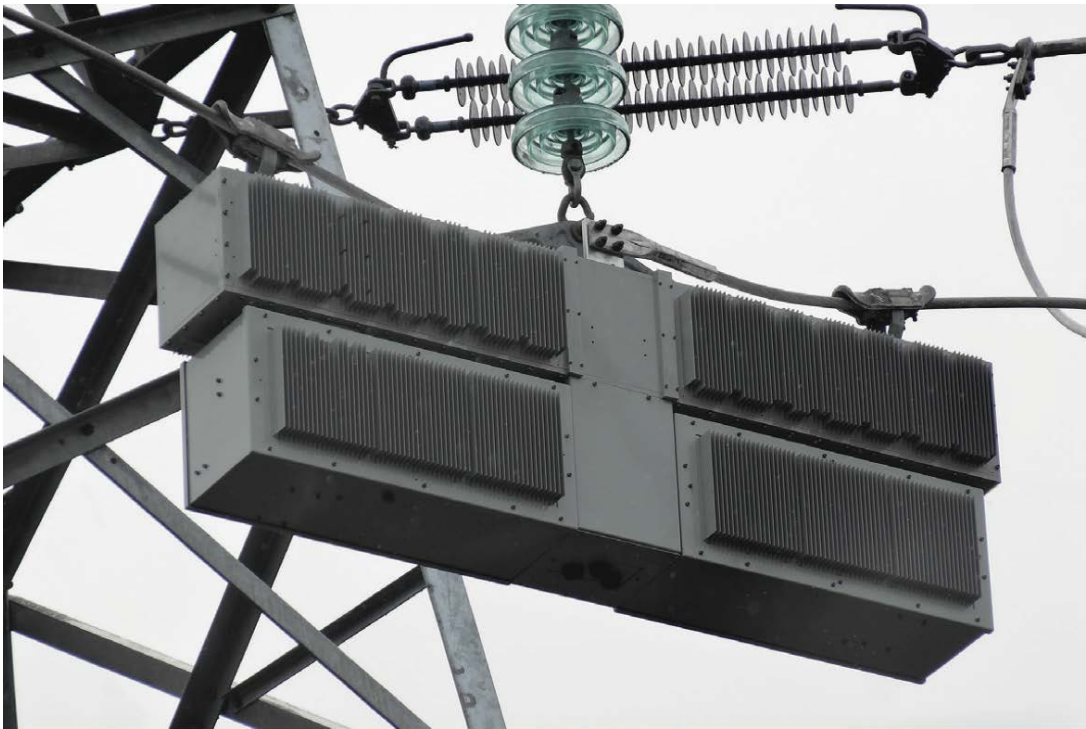
- Thyristor-Controlled Series Compensator



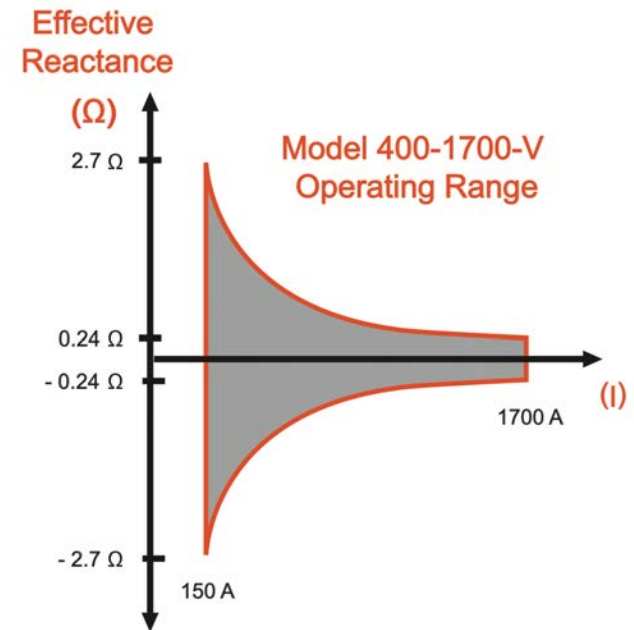


Technology – Smart Wire Grid

- Smart Wire Grid Device

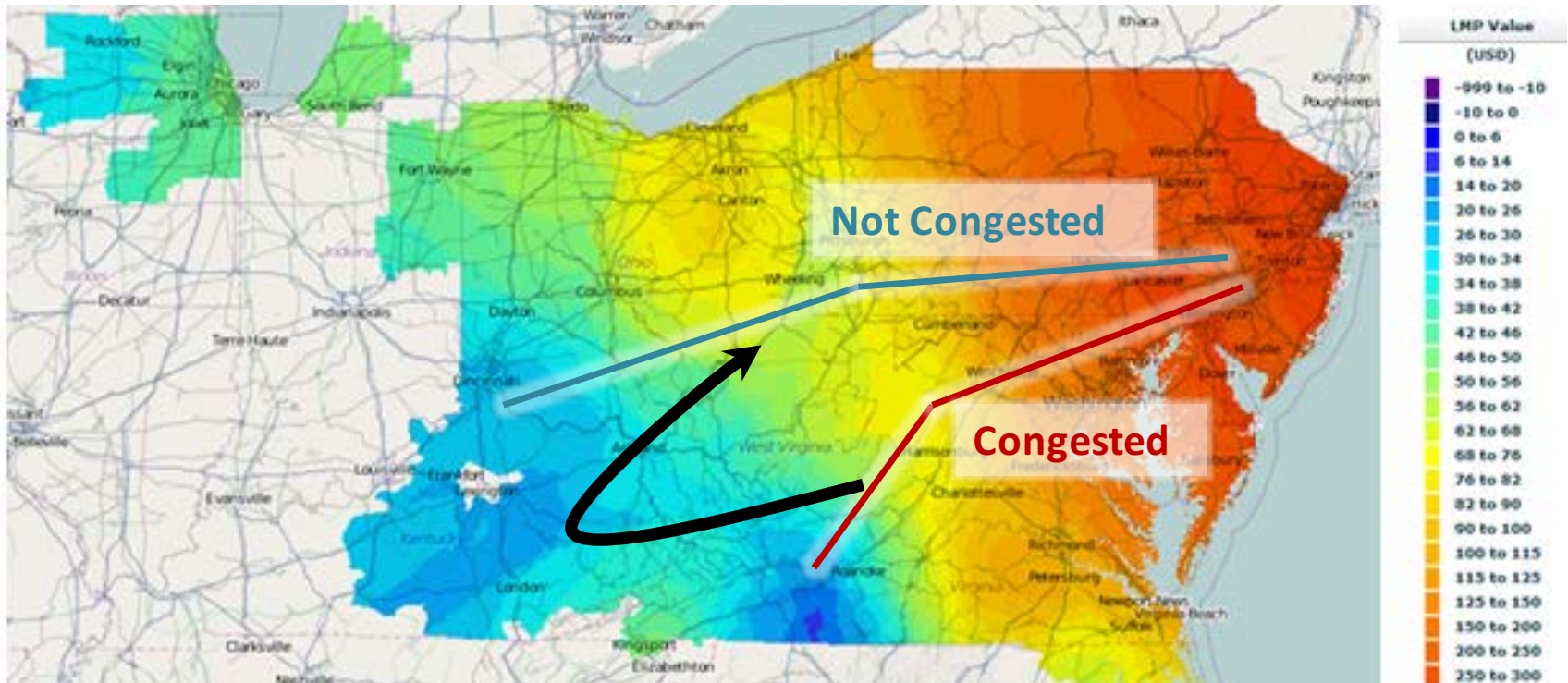


Power Router brochure





Economic Impacts



With power flow control, cheaper resources can replace the local expensive resources.



Research Objective

- Challenges:
 1. **Computational complexity** (limited time)
 2. **Power flow controllers are a part of the transmission network**
 - **Regulated**
 - **No incentive to operate in a socially optimal way**
- **Goal:** Design a market mechanism that would allow power electronics to participate in the market!



COMPUTATIONAL COMPLEXITY



Computational Complexity – DCOPF

- DCOPF – Linear Program (LP)

$$\min \sum_g c_g P_g \quad (1)$$

$$P_g^{\min} \leq P_g \leq P_g^{\max} \quad \forall g \quad (2)$$

$$-F_k^{\max} \leq F_k \leq F_k^{\max} \quad \forall k \quad (3)$$

$$F_k - B_k (\theta_n - \theta_m) = 0 \quad \forall k \quad (4)$$

$$\sum_{k \in \sigma^+(n)} P_k - \sum_{k \in \sigma^-(n)} P_k + \sum_{g \in g(n)} P_g = d_n \quad \forall n \quad (5)$$

Linear Program



Variable Impedance FACTS

Computational Burden



No FACTS set point adjustment within EMS or MMS software



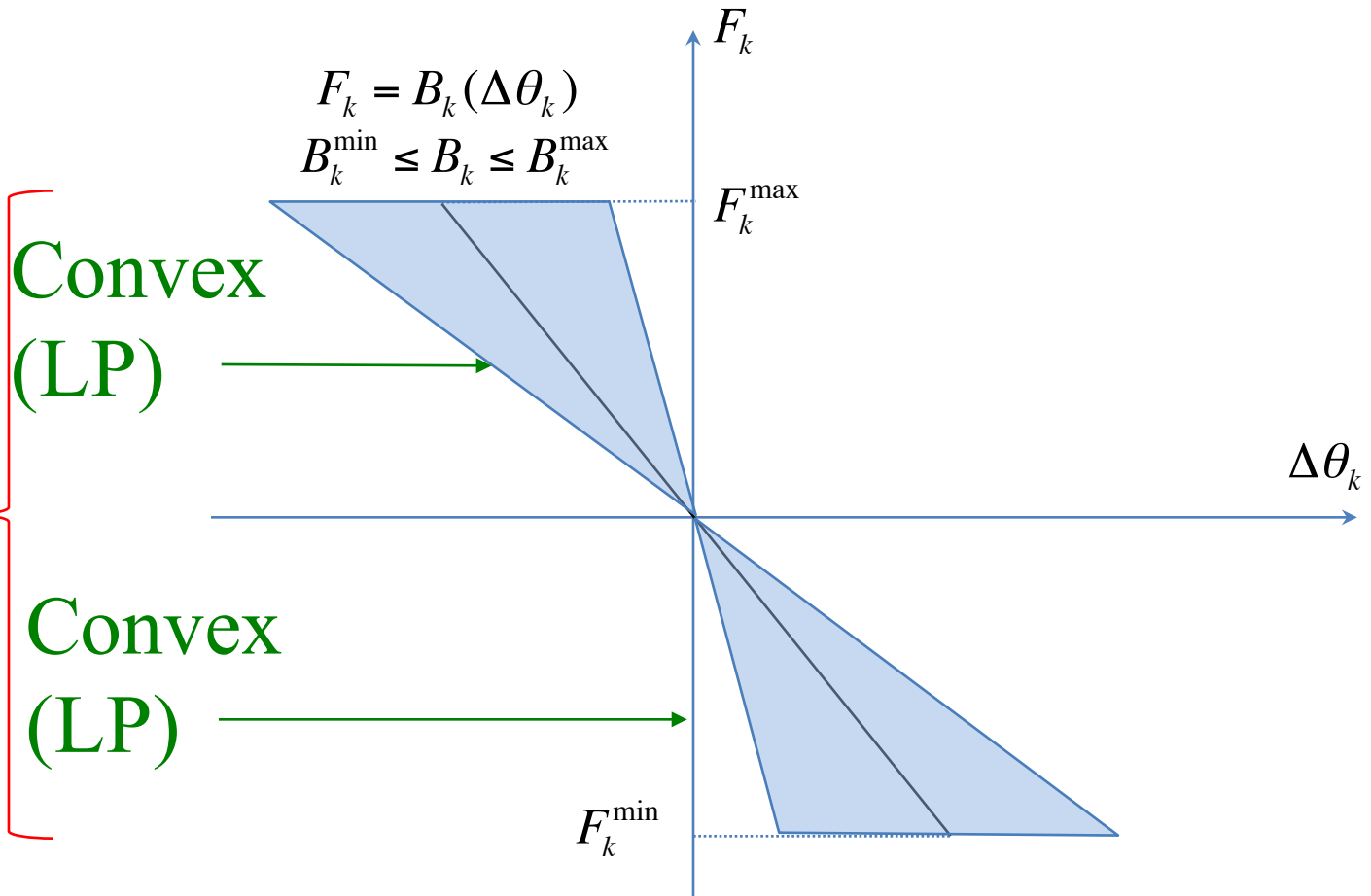
Infrequent ad hoc adjustments

- Variable impedance FACTS
 $F_k = B_k(\theta_j - \theta_i)$
 $B^{\min} \leq B \leq B^{\max}$
Nonlinear equation
Susceptance is a variable
- Provide power flow control
- Create nonlinearities in DC optimal power flow
Linear approximation (constant susceptance)



Computational Complexity – NLP/MIP

Non
Convex
(MIP)





What if we knew which B&B tree node is the optimal node?



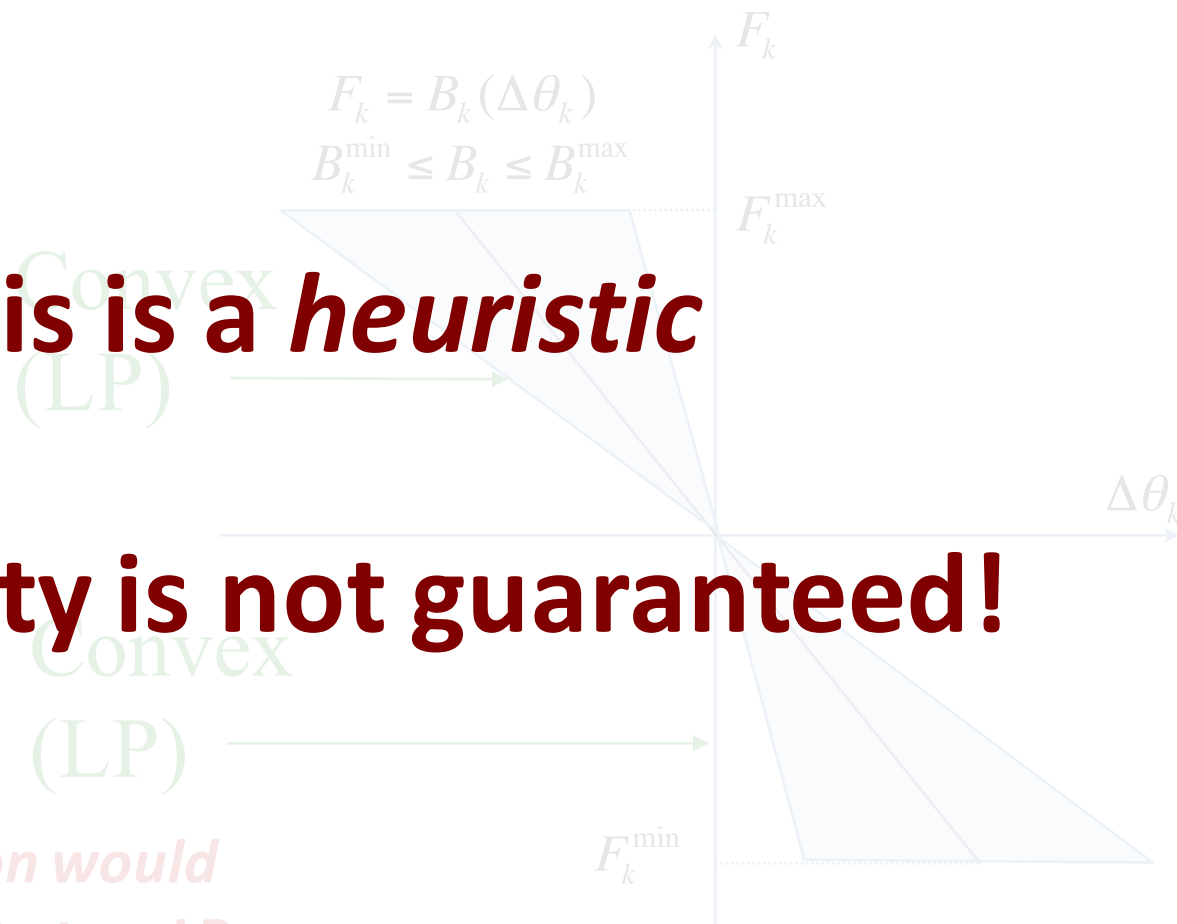
Engineering Insight

- We only need to know the direction of the power flow
- We know this direction for major lines (COI)
- *Even if we do not know the direction, we can run a two-stage DCOPE and identify*

This is a heuristic

Optimality is not guaranteed!

Knowing the direction would reduce the complexity to a LP

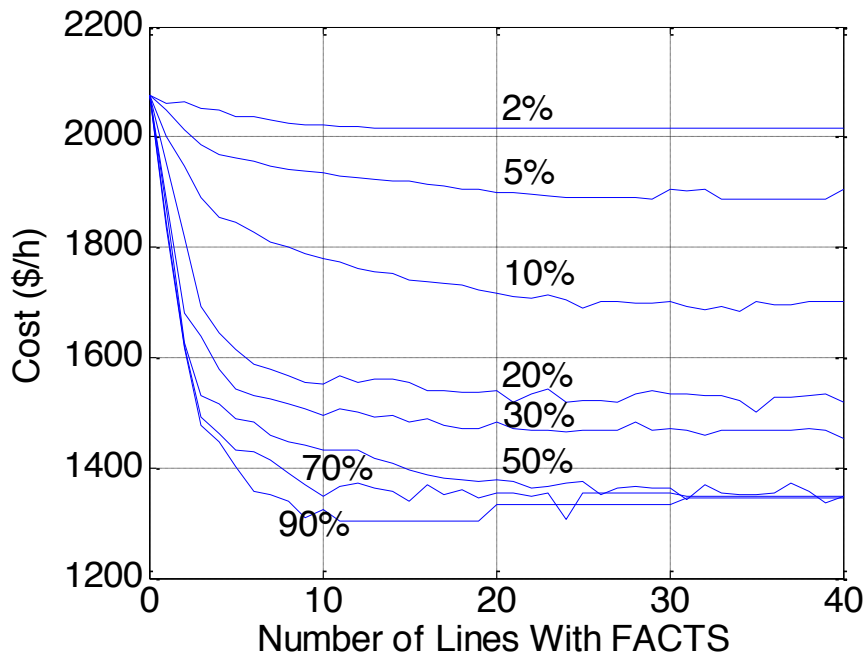




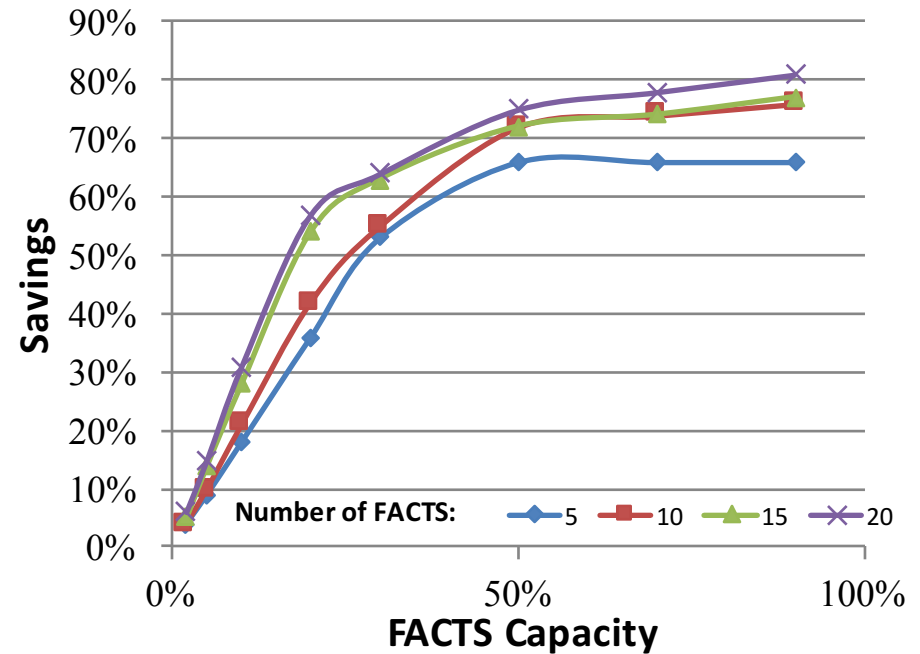
SCED Cost Savings IEEE 118-Bus System

Savings are calculated compared to a transportation model

Optimal FACTS Placement:
>98% Optimal



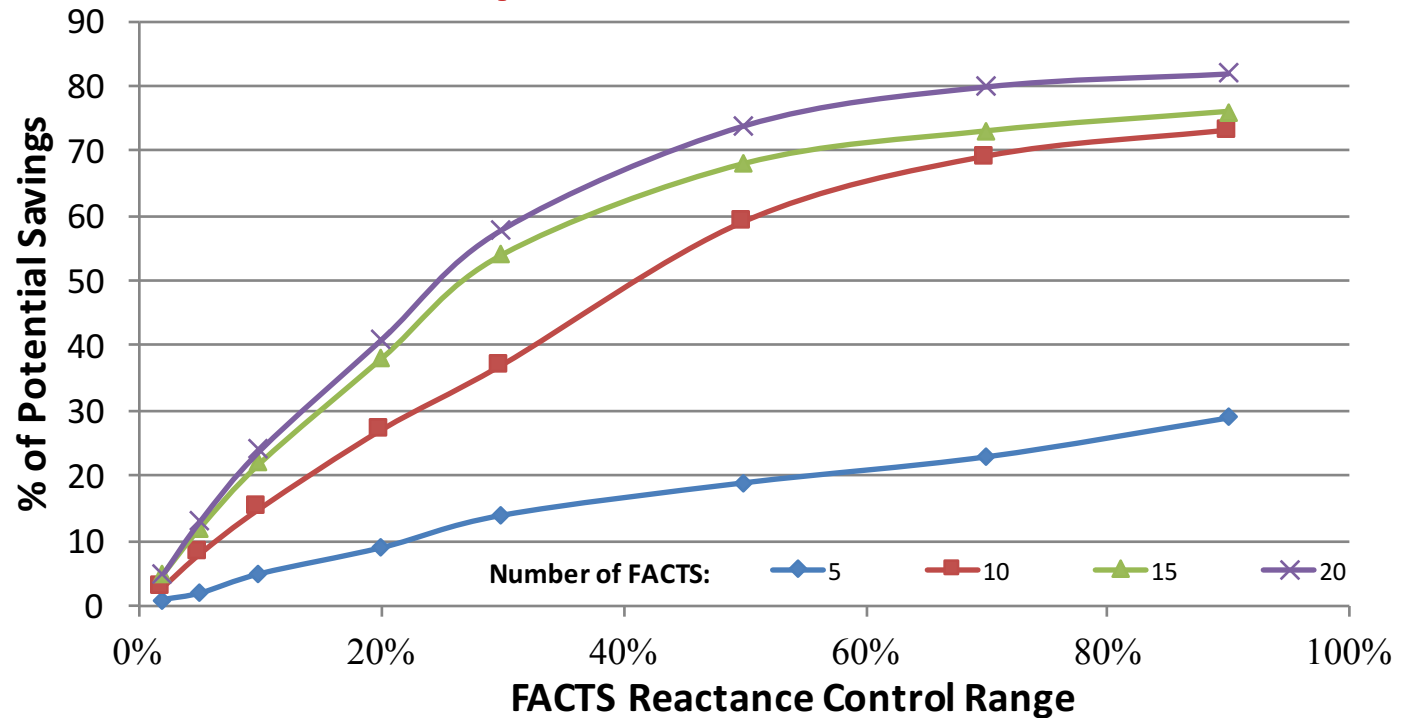
Located on More Heavily Utilized Lines: 100% Optimal





SCED Cost Savings Polish System

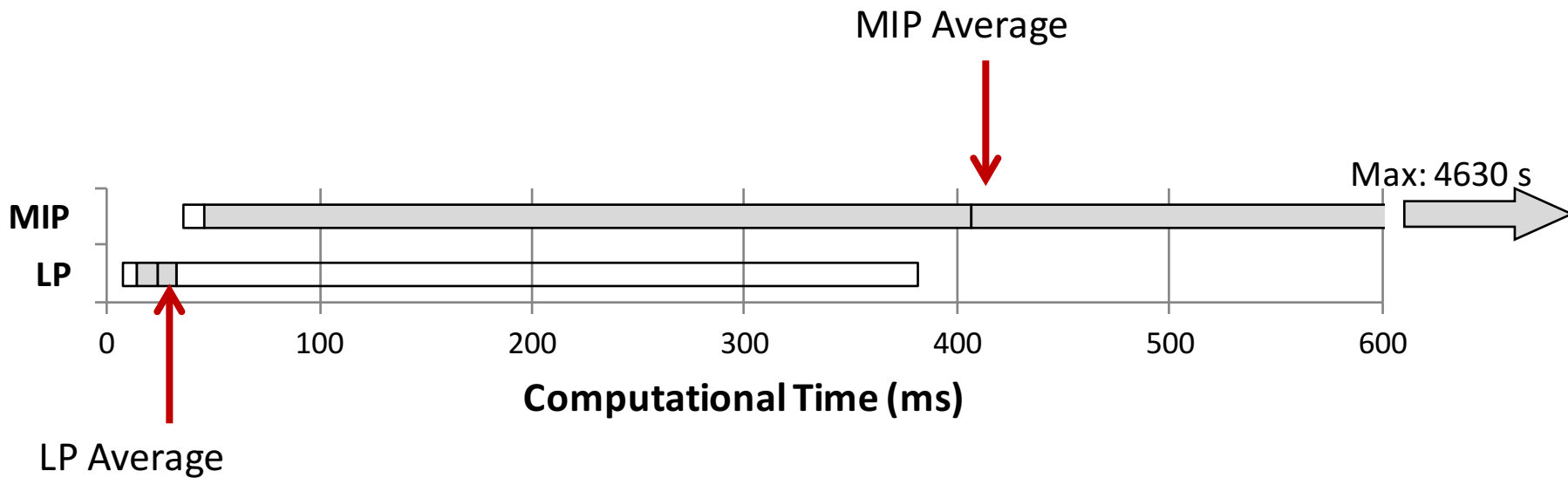
**Located on More Heavily Utilized Lines: 100%
Optimal**



Savings are calculated compared to a transportation model



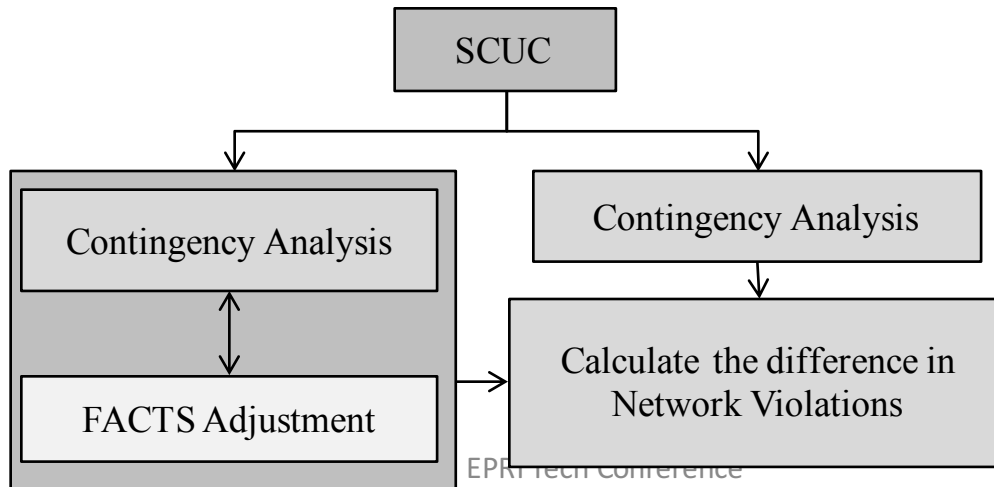
Computational Time





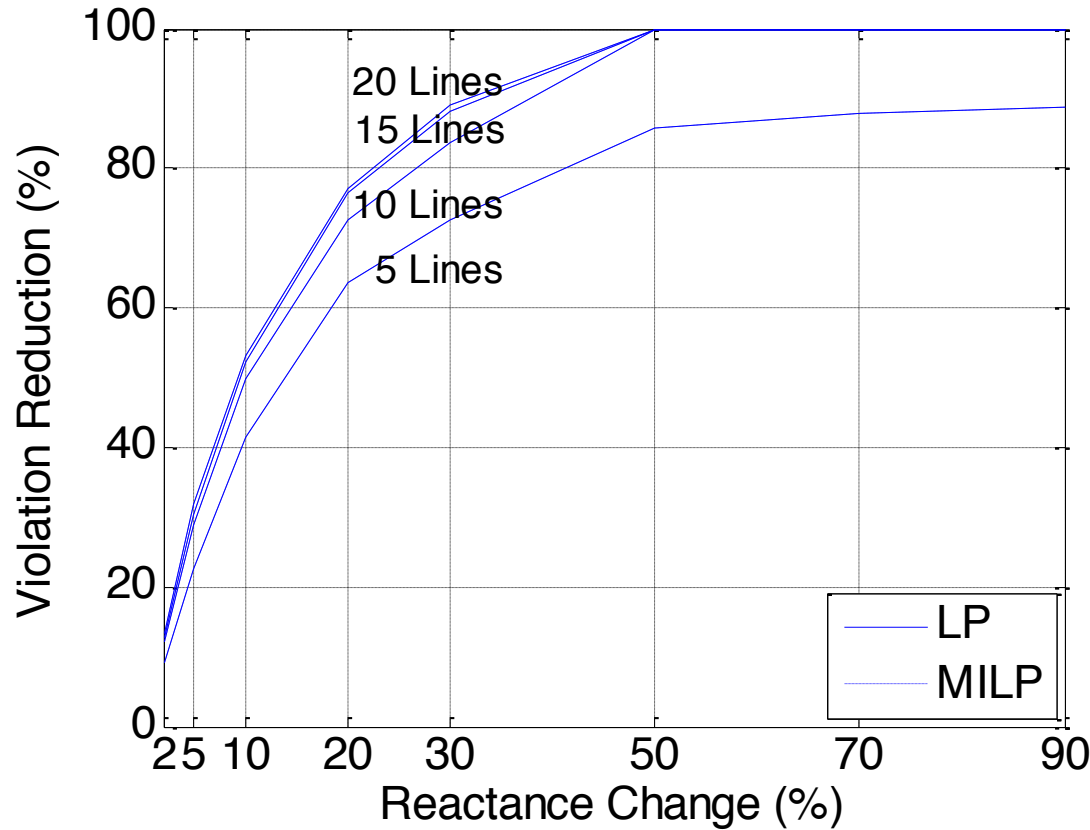
Corrective Adjustments

- In corrective adjustments we have even better insight about the direction of the power flow: pre- or post- contingency flows
- Goal: minimization of post-contingency network violations
- **Optimal utilization of FACTS in recourse state only**





Corrective Results IEEE 118-Bus System

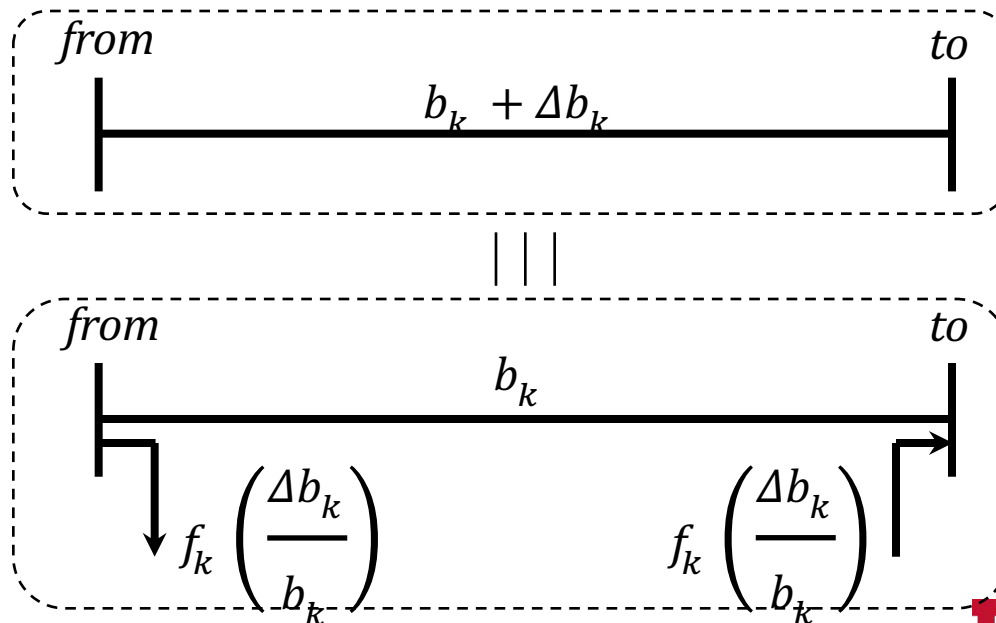


Located on More
Heavily Utilized
Lines:
100% Optimal



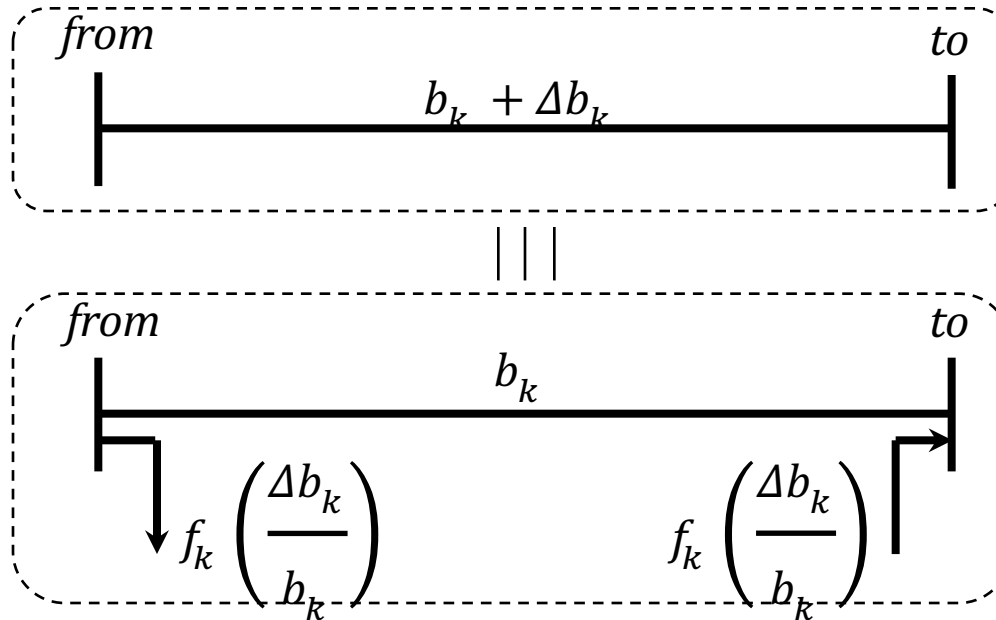
Shift Factor Structure

- Industry implementations of SCUC and SCED do not use $B\theta$ structure; they use PTDFs.
 - No need to model all the voltage angles
 - No need to calculate all the flows
 - Significantly faster compared to $B\theta$





Injection Model of Reactance Control

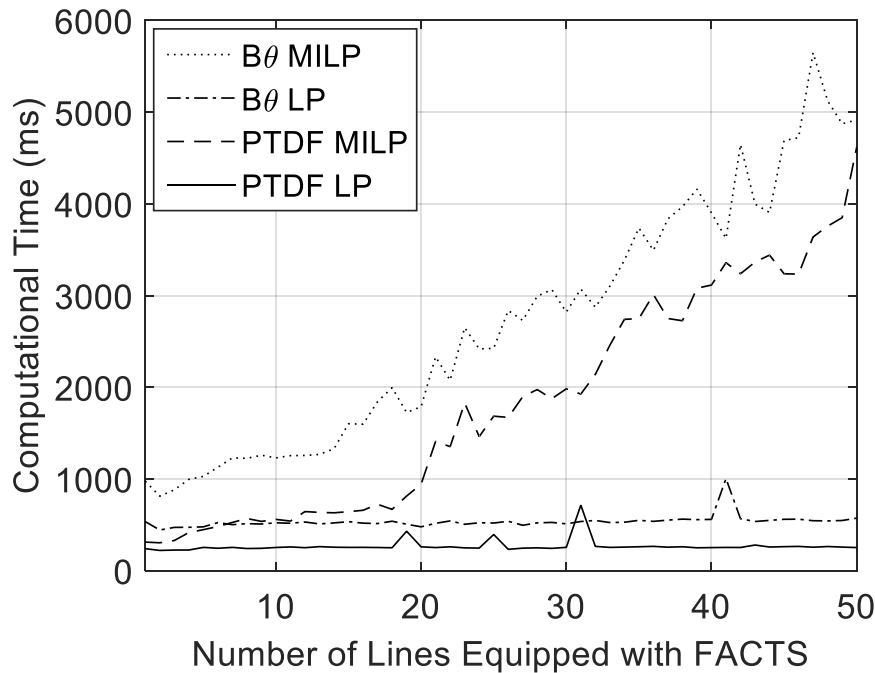


- **Again, we end up with a Mixed-Integer Linear Program!**
- **We can use the same engineering insight to convert this to a LP.**
- **Similar method can be used to generate contingency constraints.**

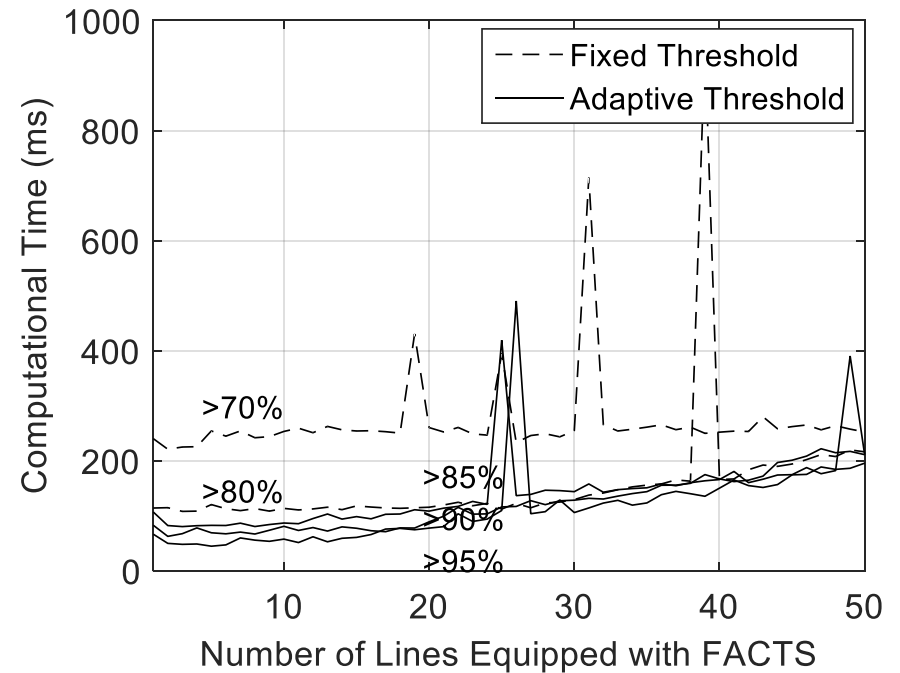


Results – Polish System

$B\theta$ versus PTDF



Fixed versus Adaptive Thresholds



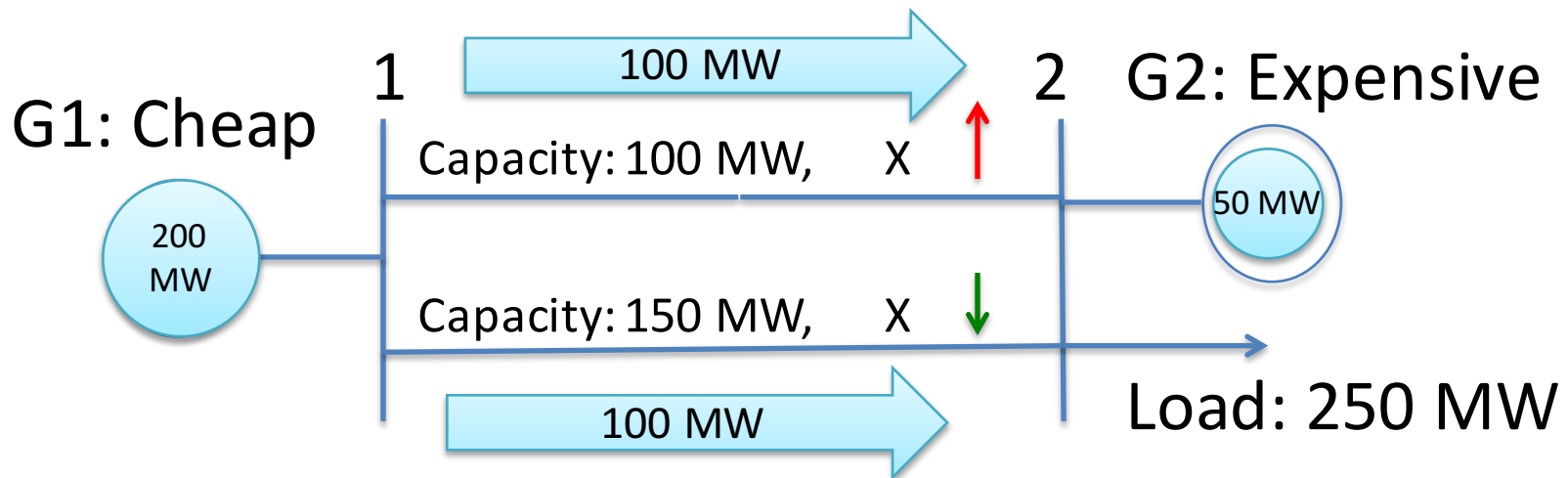


MARKET PARTICIAPTION



O'Neill's Complete Market Proposal

- Positive externality in Dr. O'Neill's complete market proposal:
 - **Payment to line: (Flow) x (LMP Difference)**
- **No matter which line changes the reactance, it is always the second line that will carry more power and get paid!**





Proposed Payment System

- Use the susceptance price to calculate the marginal value of susceptance:

$$F_k = B_k (\theta_j - \theta_i) \quad (S_k)$$

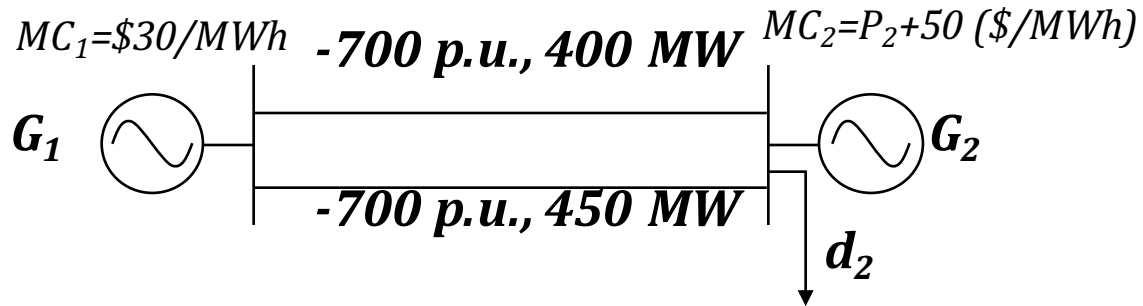
$$S_k (\theta_j - \theta_i) \times \Delta B_k$$

Marginal Value: Price

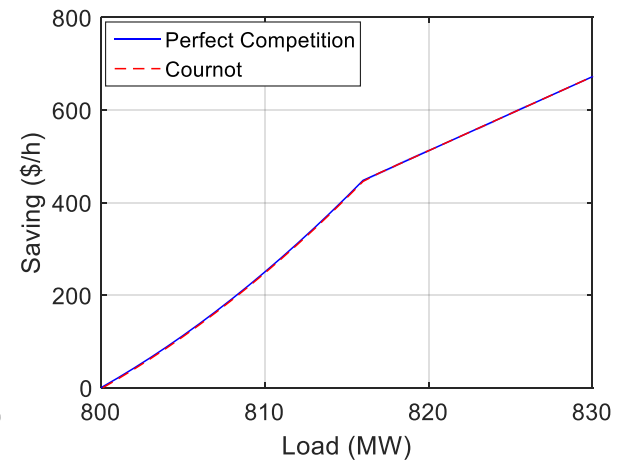
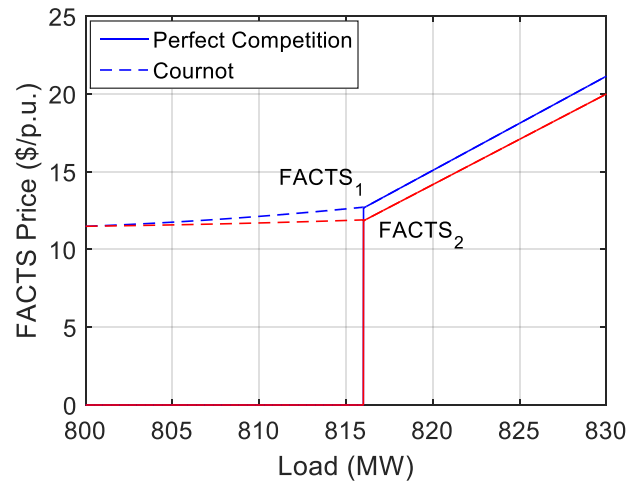
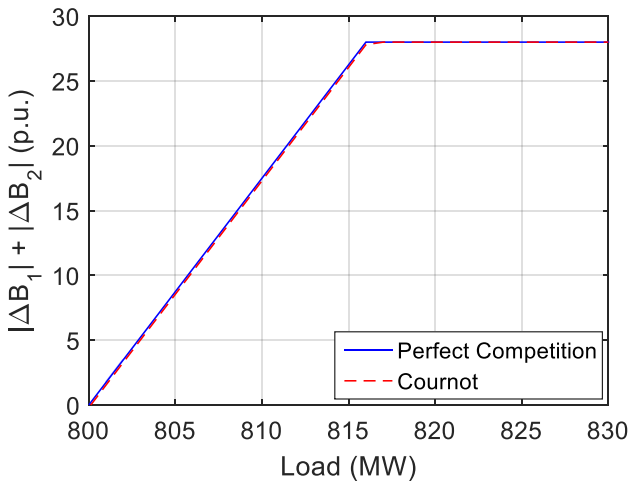
Quantity



Two Node System

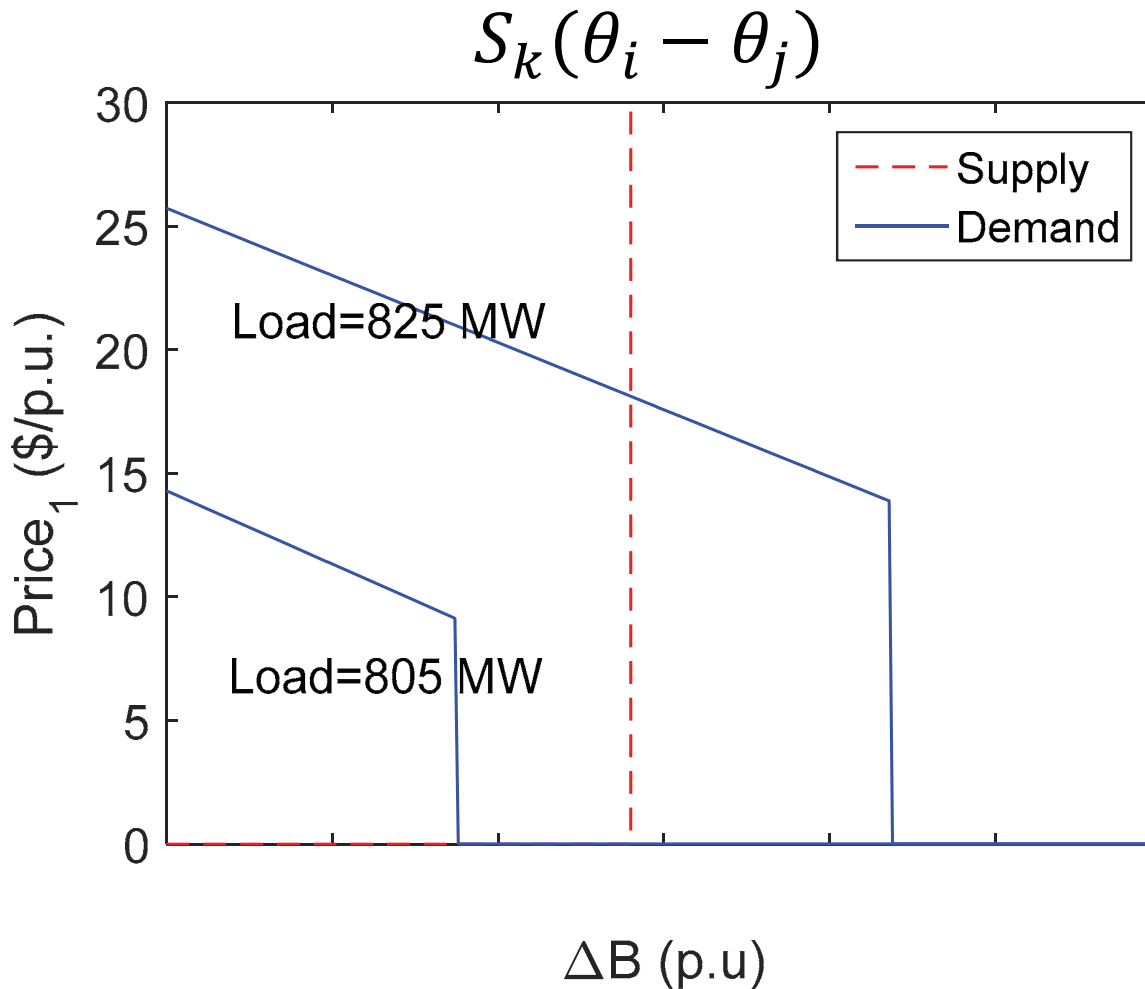


FACTS control range: 2%





Marginal Value





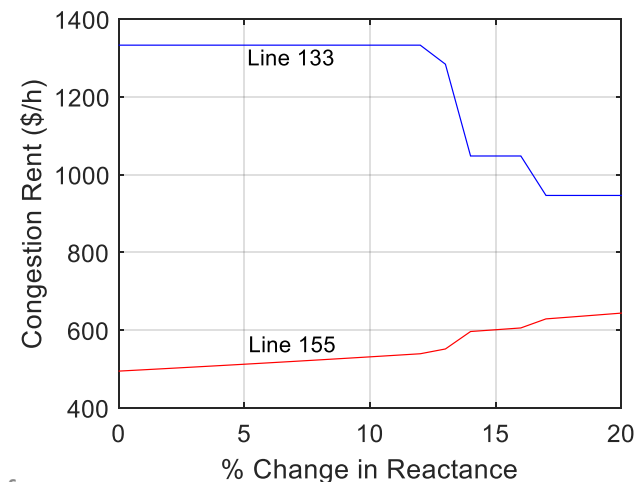
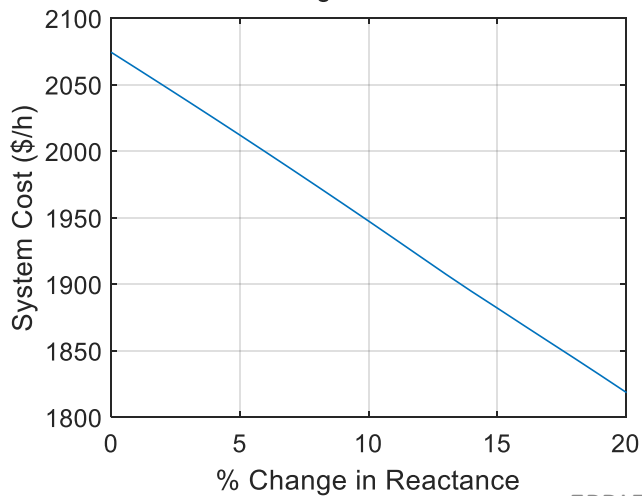
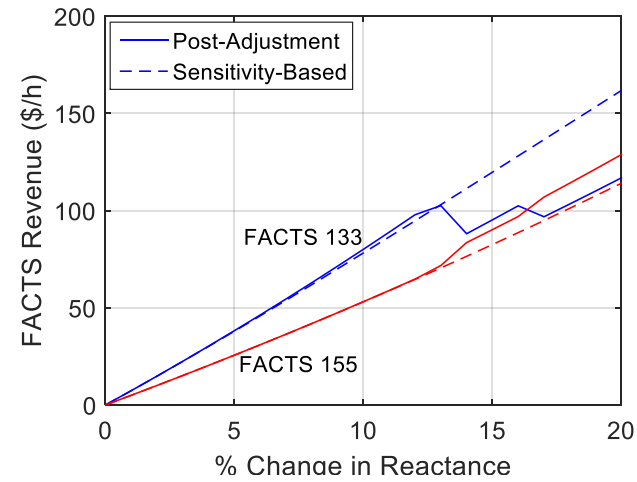
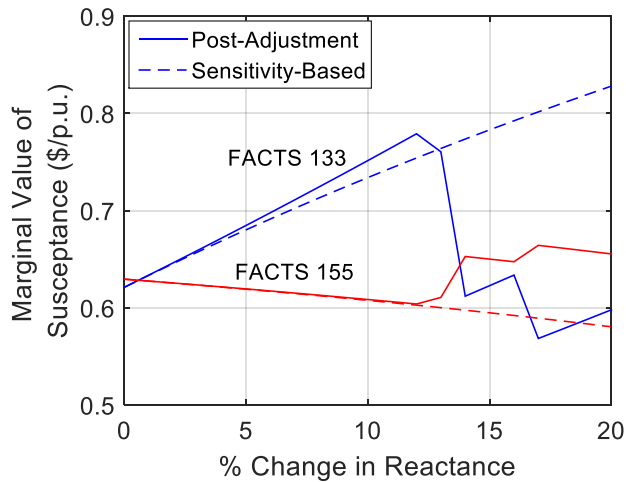
Revenue Adequacy

- **Congestion rent is the payment source**
- **Revenue adequate if the adjustments lead to increased loading!**
- **Not necessarily guaranteed in all cases**
- **It is highly unlikely that the market is revenue inadequate**



IEEE 118 Bus System

2 FACTS Devices





Conclusions

- Mathematical representation of OPF with FACTS: NLP
- We reformulated the NLP to a MILP; using our knowledge of electricity flow physics, we reformulate the problem to an LP
- The LP heuristic is extremely effective: it found the optimal solution more than 98% of the time.
- The heuristic is extremely fast (LP) and would not add to the complexity of the OPF problem
- We designed a compensation mechanism to signal enhanced operation of the devices.



Thank you!

Questions?

Mostafa Sahraei-Ardakani

mostafa.ardakani@utah.edu

- M. Sahraei-Ardakani and K. Hedman, "A Fast LP Approach for Enhanced Utilization of Variable Impedance Based FACTS Devices," *IEEE Transactions on Power Systems*
- M. Sahraei-Ardakani and K. Hedman, "Day-Ahead Corrective Adjustment of FACTS Reactance: A Linear Programming Approach," *IEEE Transactions on Power Systems*
- M. Sahraei-Ardakani and S. Blumsack, "Transfer Capability Improvement through Market-Based Operation of Series FACTS Devices," *IEEE Transactions on Power System*
- M. Sahraei-Ardakani and K. Hedman, "Computationally Efficient Adjustment of FACTS Set Points in DC Optimal Power Flow with Shift Factor Structure," *IEEE Transactions on Power Systems*